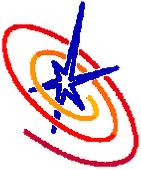


## Explosive Astrophysics with Flash

Alan Calder ([alan.calder@stonybrook.edu](mailto:alan.calder@stonybrook.edu))  
Sean Couch ([smc@flash.uchicago.edu](mailto:smc@flash.uchicago.edu))

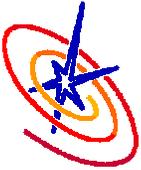
Many, many others!

HIPACC Summer School  
July 20, 2011



# Outline

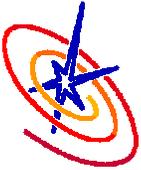
- Introducing Flash
  - Components of Flash
  - Running a simulation with Flash
  
- Simulating with Flash
  - Block Structured AMR
  - System Requirements
  - Verification and Validation: definitions and methods
  - Case studies with Flash
  - Issues relevant to performing quality simulations.
  
- Sample nuclear astrophysics problems.
  - 2-d cellular detonation
  - 1-d flame
  - 2-d white dwarf detonation



# Introducing Flash

---

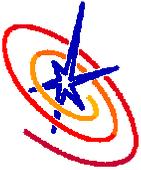
- Flash has been under development since 1997 at the Flash Center for Computational Science at the University of Chicago.
- Many, many developers.
  - Current developers: Anshu Dubey (group leader), John Bachan, Sean Couch, Chris Daley, Milad Fatenejad, Norbert Flocke, Carlo Graziani, Shравan Gopal, Cal Jordan, Dongwook Lee, Dean Townsley, Klaus Weide.
  - Past major developers: Katie Antypas, Alan Calder, Jonathan Dursi, Robert Fisher, Kevin Olson, Timur Linde, Tomek Plewa, Paul Ricker, Katherine Riley, Andrew Siegel, Dan Sheeler, Frank Timmes, Natasha Vladimirova, Greg Weirs, Mike Zingale.
- Documentation  
[http://flash.uchicago.edu/site/flashcode/user\\_support](http://flash.uchicago.edu/site/flashcode/user_support)



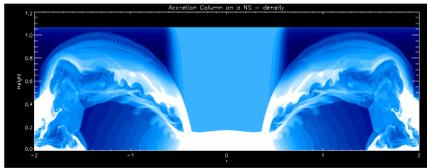
# What is Flash?

---

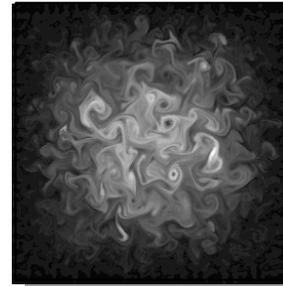
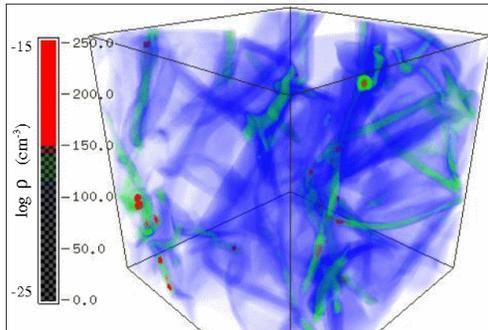
- Flash is composed of units (code modules) that are combined to construct a code for a particular application.
- Flash is written principally in Fortran, with some C and Python. The physics units are in Fortran.
- A setup script performs the steps to construct the code for an application. It processes information in configuration scripts for a particular problem and for the units. It also takes arguments.
- Flash applications include
  - Nuclear astrophysics
  - Cosmology
  - Fluid dynamics
  - High energy density physics



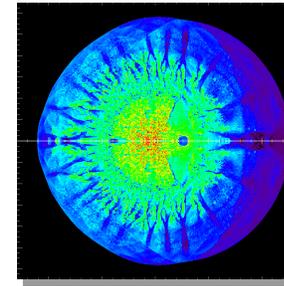
# The FLASH Code



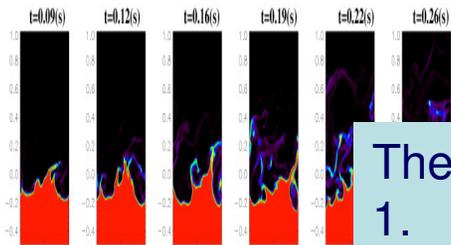
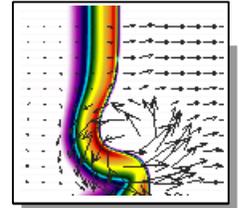
Shortly: Relativistic accretion onto NS



Compressed turbulence Type Ia Supernova



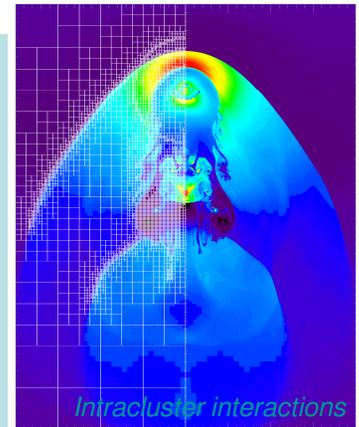
Flame-vortex interactions



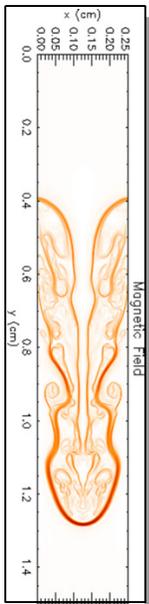
Wave breaking on white dwarf

## The FLASH code

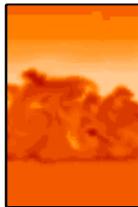
1. Parallel, adaptive-mesh simulation code
2. Designed for compressible reactive flows
3. Solves reactive Euler equations using the PPM
4. Included self-gravity
5. Newly-implemented HED capabilities
6. Newly-implemented MHD capabilities.
7. Scales and performs well.
8. Is available on the web: <http://flash.uchicago.edu>



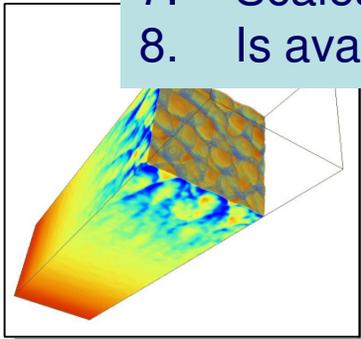
Intracluster interactions



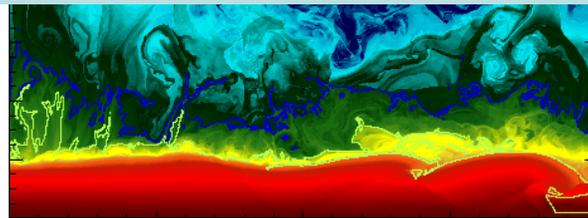
Magnetic Rayleigh-Taylor



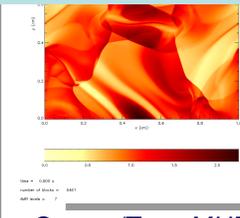
Nova outburst



Cellular detonation



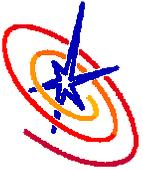
Helium burning on neutron stars



Orszag/Tang MHD vortex



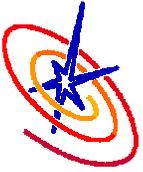
Richtmyer-Meshkov instability



# Flash Infrastructure Capabilities

---

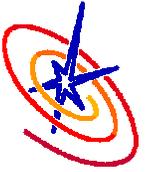
- Configuration (setup)
- Mesh Management
  - PARAMESH- block structured AMR
  - Chombo- patch based AMR
  - Uniform grid
- Parallel I/O
  - HDF 5
  - PnetCDF
  - Fortran
- Monitoring
- Performance monitoring
- Verification testing
  - Unit
  - Regression



# Flash Physics

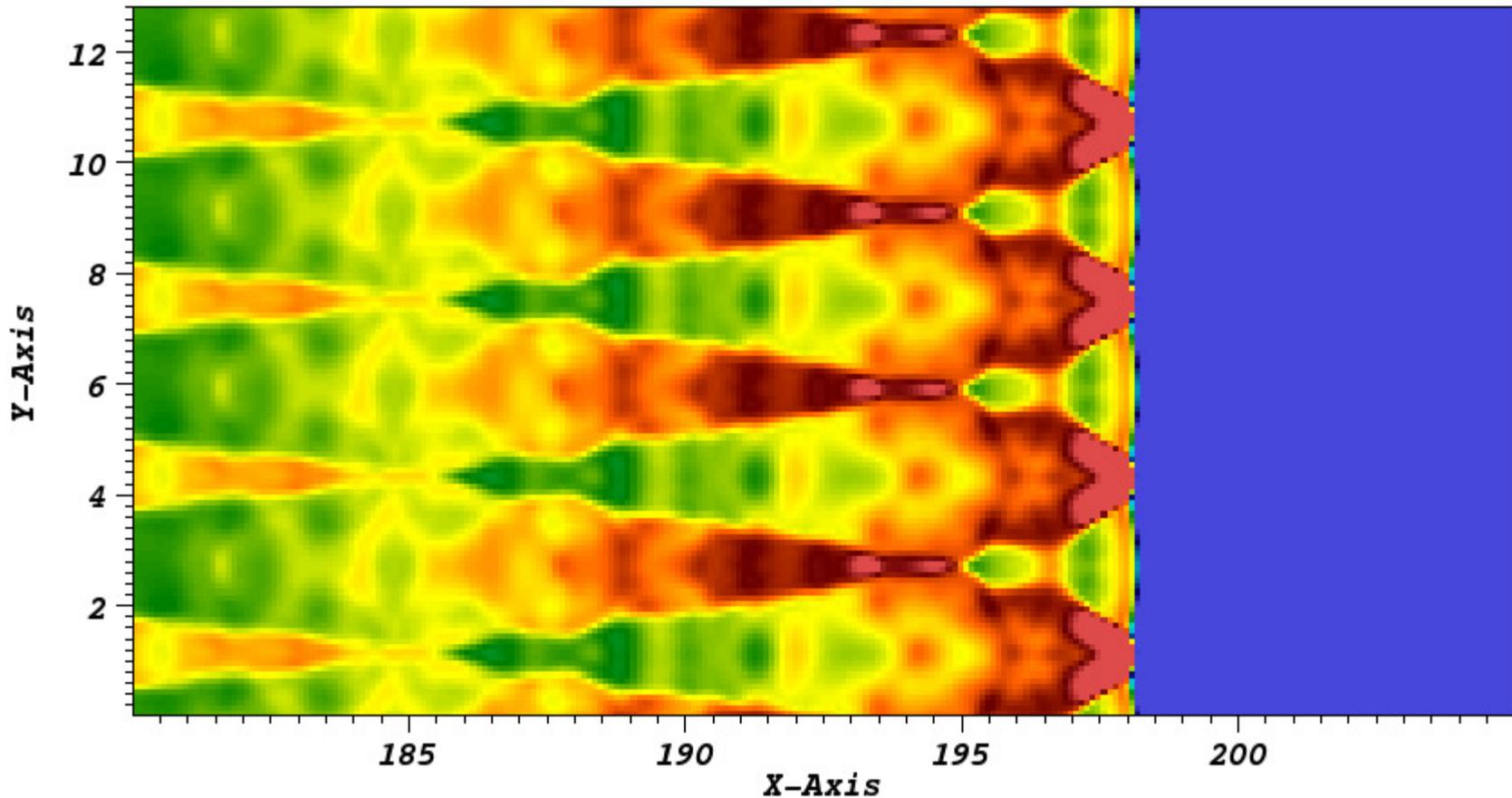
---

- Flash Units:
  - Hydrodynamics, MHD, RHD
  - Material equations of state
  - Nuclear physics and other source terms
  - Gravity- applied and self-gravitating
  - Material properties
  - Cosmology
  - High energy density
  
- Particles
  - Lagrangian tracers
  - Active (massive)

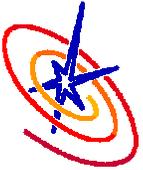


# Example: Cellular Detonation Problem

- Nuclear astrophysics example : a cellular detonation.



Problem described in Timmes et al. ApJ 543 938 (2000)



# Running Flash I

---

Move to the project directory

```
cd /project/projectdirs/training/HIPACC_2011/calder/
```

Unpack the tar file

```
tar xzvf FLASH4-alpha
```

Move to the directory in which the code resides

```
cd FLASH4-alpha
```

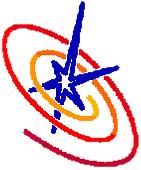
Run the setup script to set up the cellular detonation problem

```
./setup Cellular -auto -site=hopper.nersc.gov
```

Move into the newly-created object directory and compile the code

```
cd object
```

```
make
```



# Running Flash I

- Important note: One can set many parameters at setup time to tailor the simulation for the architecture, etc.
- An example is maxblocks, which sets the maximum number of blocks per processor element. Recall Katie Antypas's point about the memory per core decreasing from Franklin to Hopper. Must account for this!

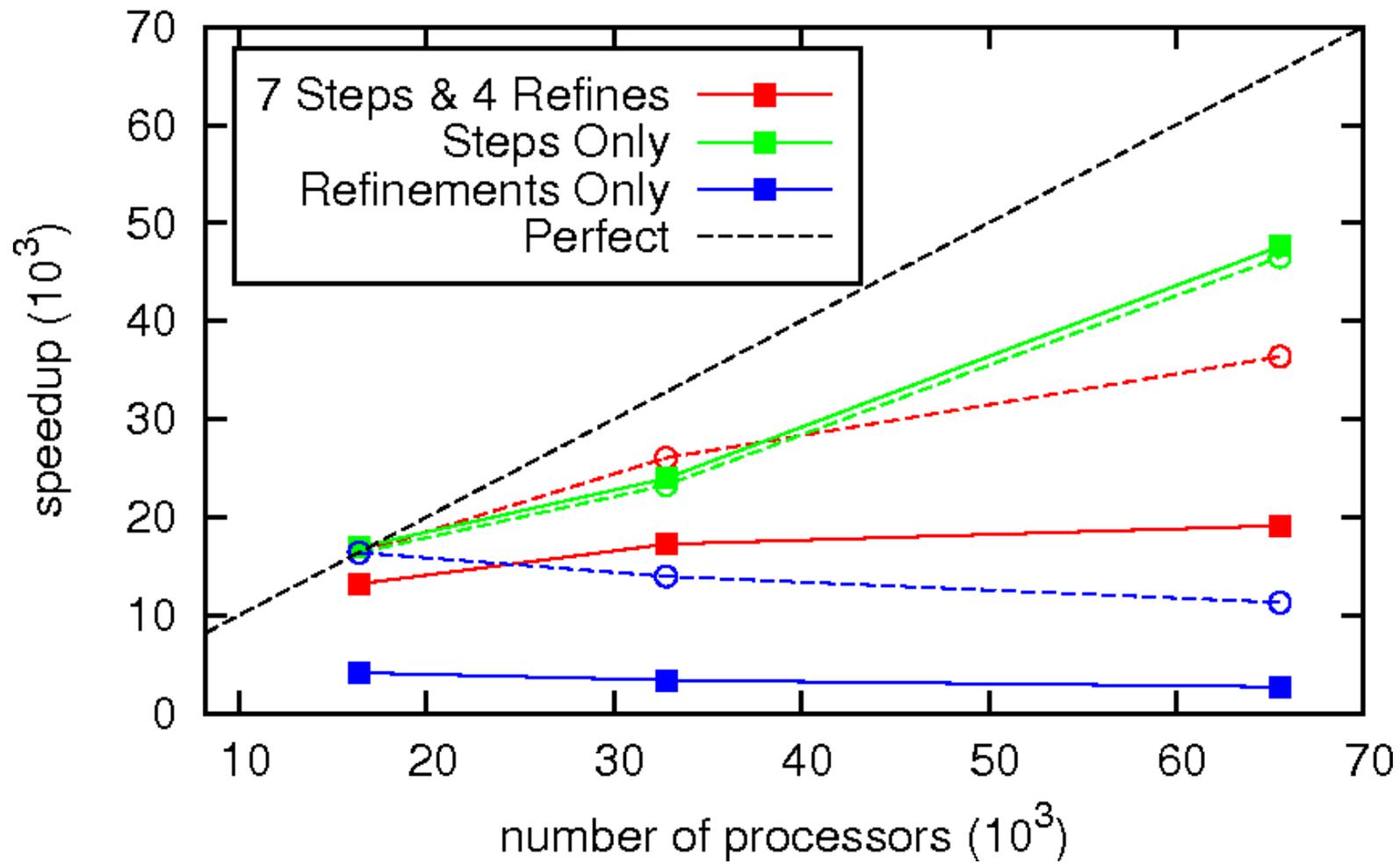
```
./setup Cellular -auto -site=hopper.nersc.gov -  
objdir=obj_cellular2 -maxblocks=200
```

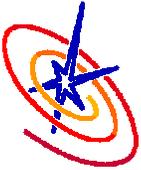
- More on estimating the memory utilization later.



# Performance Example

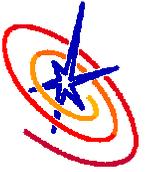
Strong Scaling on Intrepid - BG/P



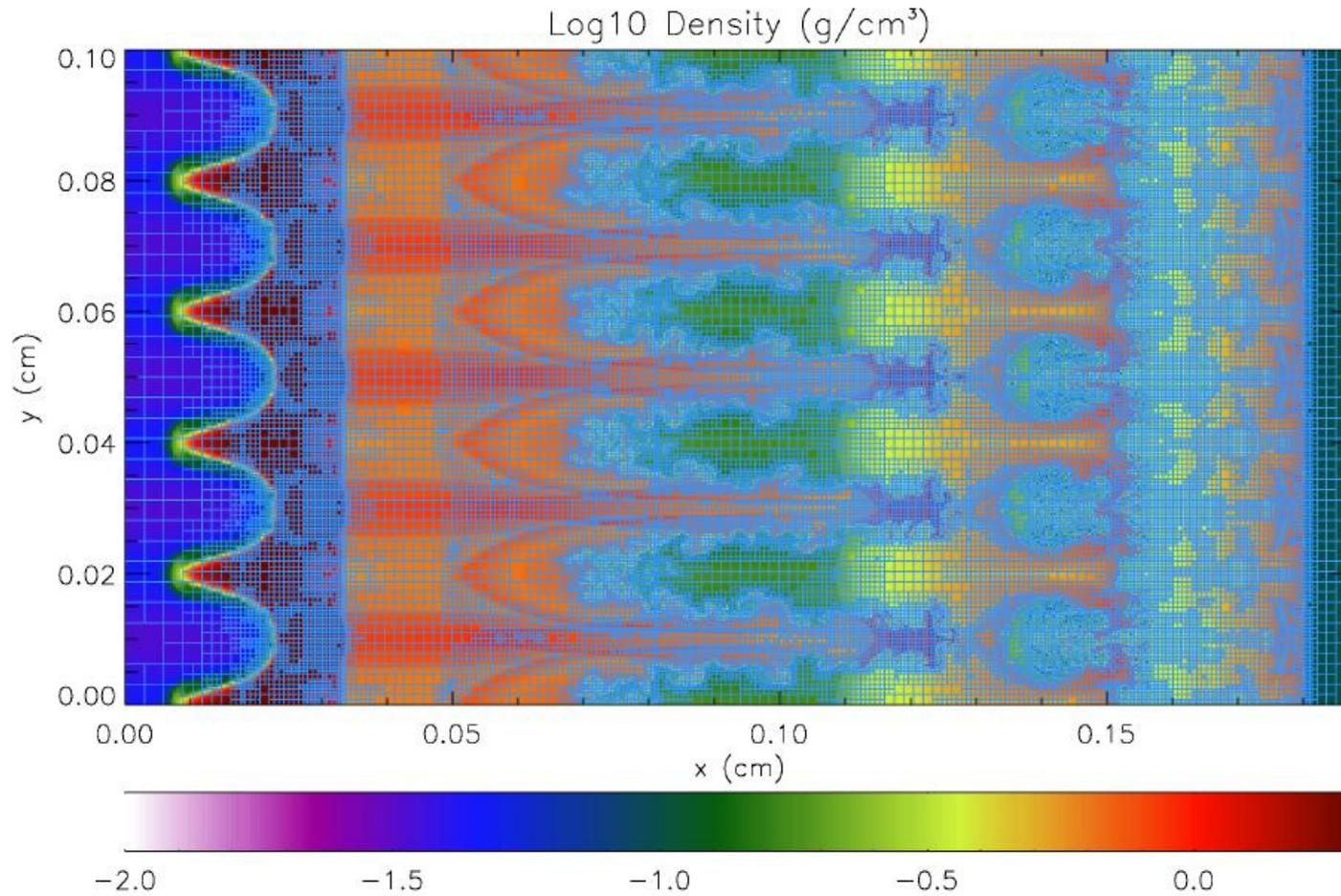


# Adaptive Mesh Refinement

- AMR seeks to minimize computational expense by adding resolution elements only as needed to resolve features in the flow.
- Flash uses a block-structured approach to AMR.
- The simulation domain is divided into a series of logically-Cartesian blocks with the resolution set by the number of blocks in a region of physical space.
- The number of blocks changes (adapts) via a parent-child relationship.
- The mesh package (e.g. PARAMESH)
  - Manages the creation of grid blocks
  - Builds and maintains the tree structure that tracks the spatial relationship between blocks
  - Distributes blocks among available processors
  - Handles inter-block and inter-processor communication.
  - Tracks physical boundaries and enforces boundary conditions

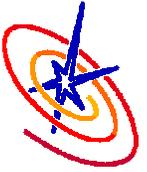


# Adaptive Mesh Refinement

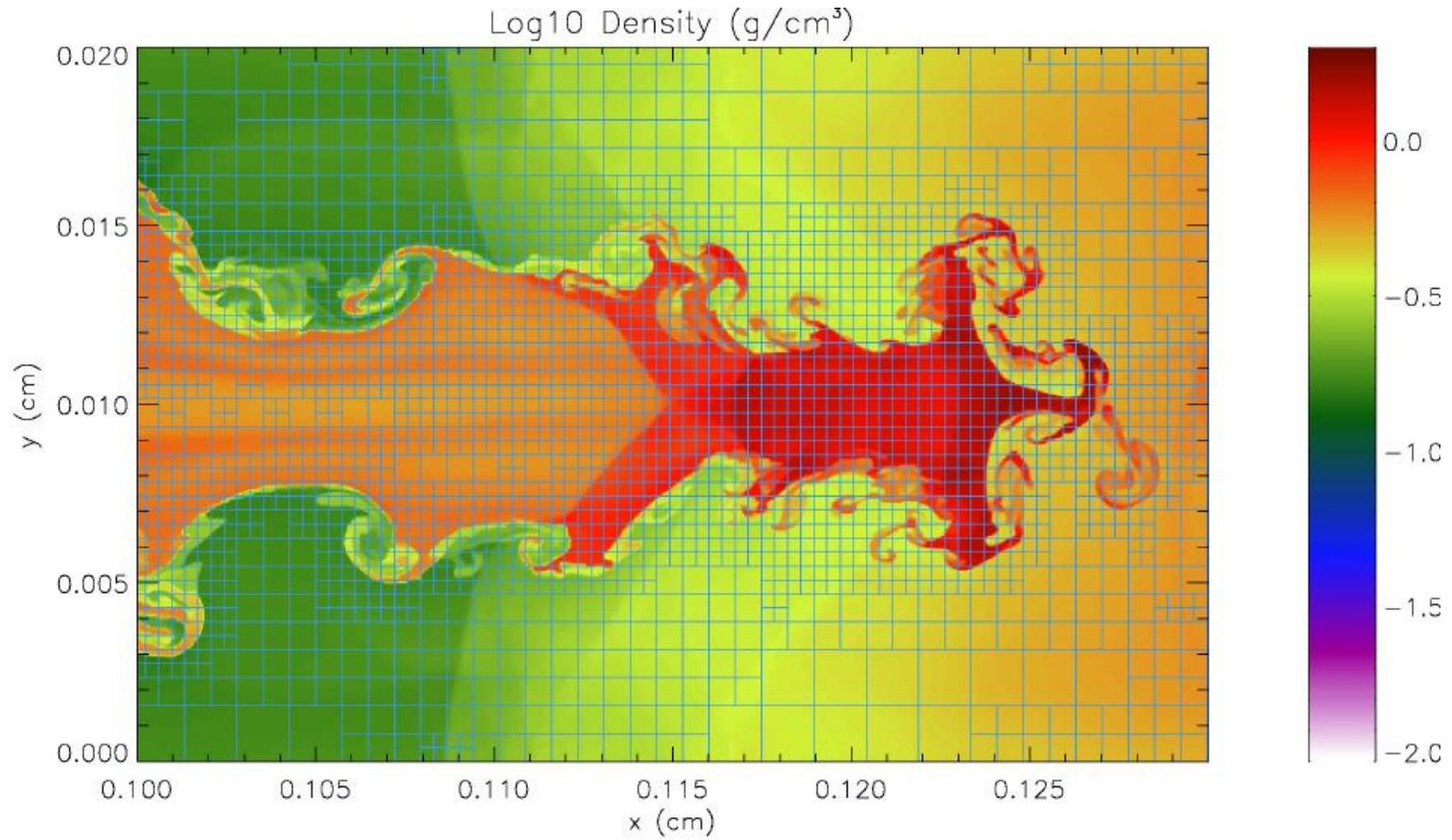


time = 64.001 ns  
number of blocks = 90166, AMR levels = 9

/scratch4/calder/new\_val\_res\_study/work\_2048/3lay\_hdf\_plt\_cnt\_0064

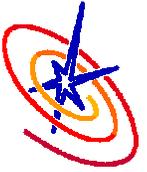


# Adaptive Mesh Refinement

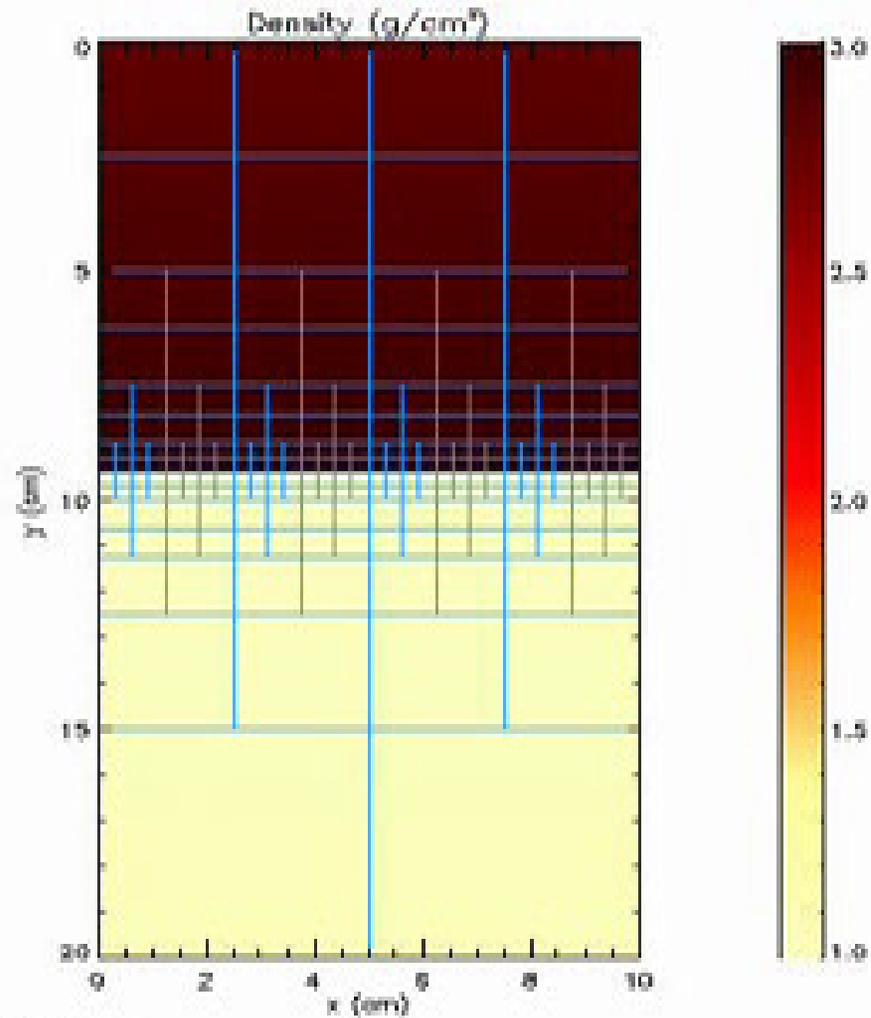


time = 64.001 ns  
number of blocks = 90166, AMR levels = 9

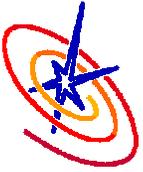
/scratch4/calder/new\_val\_res\_study/work\_2048/3lay\_hdf\_pit\_cnt\_0064



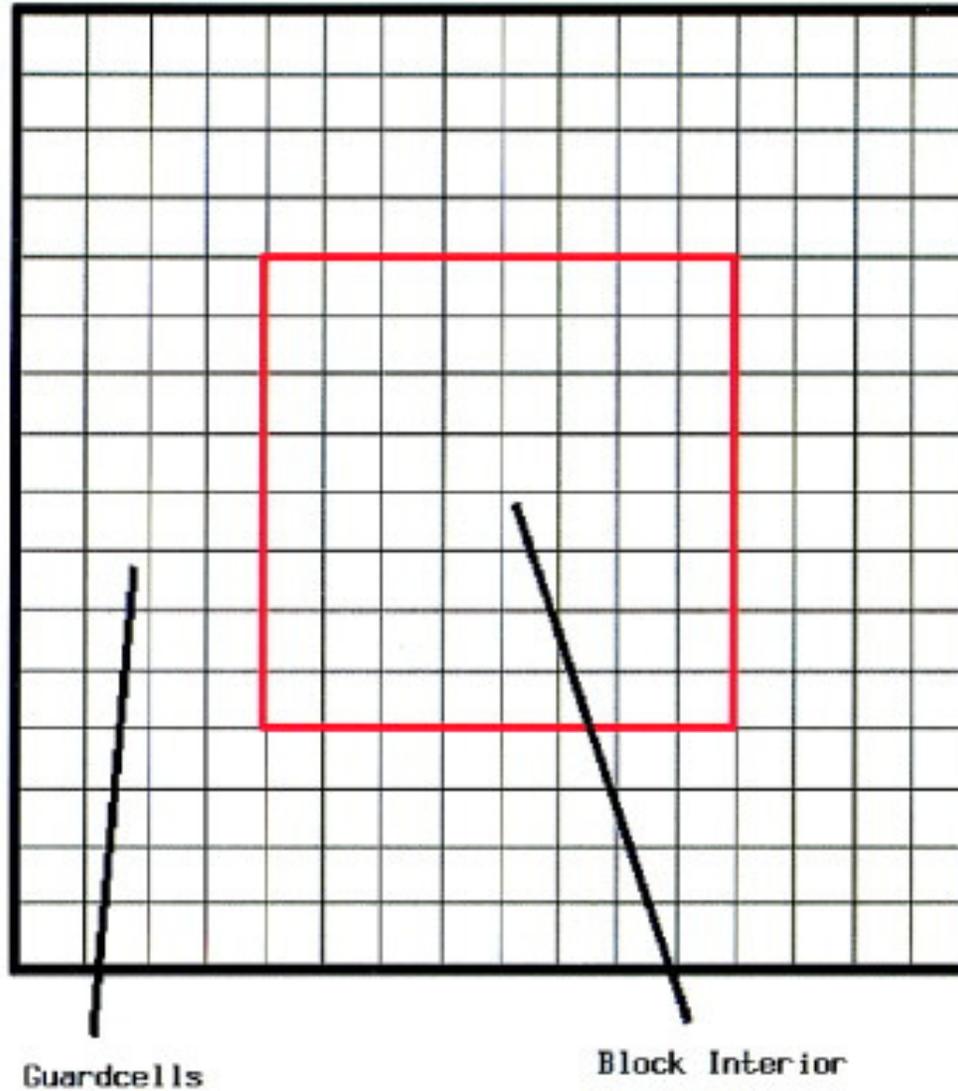
# Adaptive Mesh Refinement



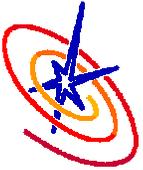
time = 0.000 ps  
number of blocks = 308  
AMR levels = 8



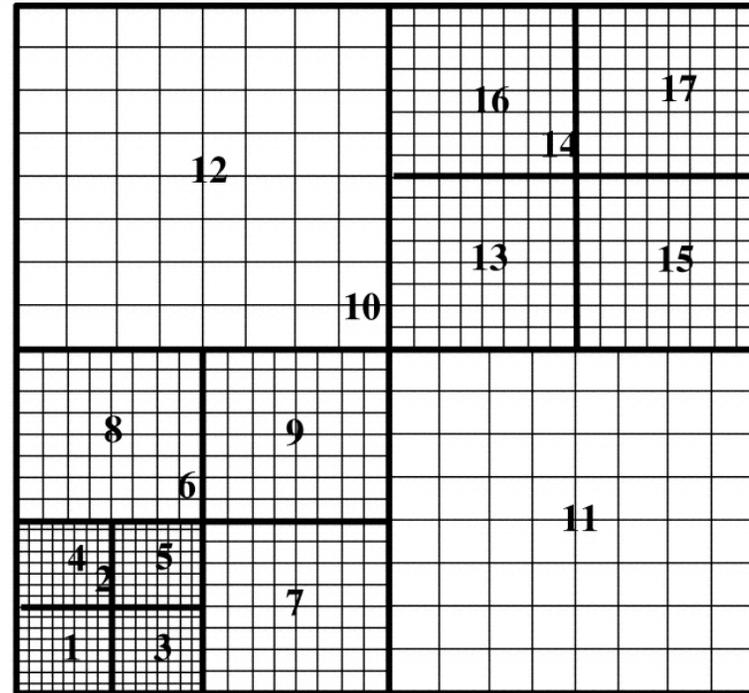
# Example Block



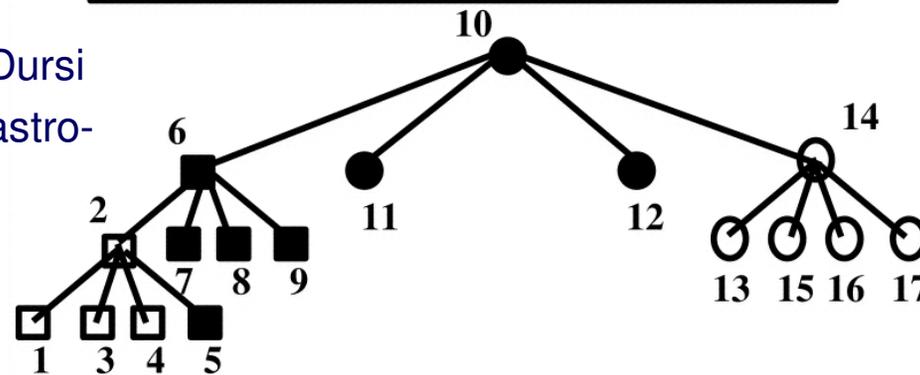
From Fryxell et al. ApJS 131 273 (2000)



# Example Domain



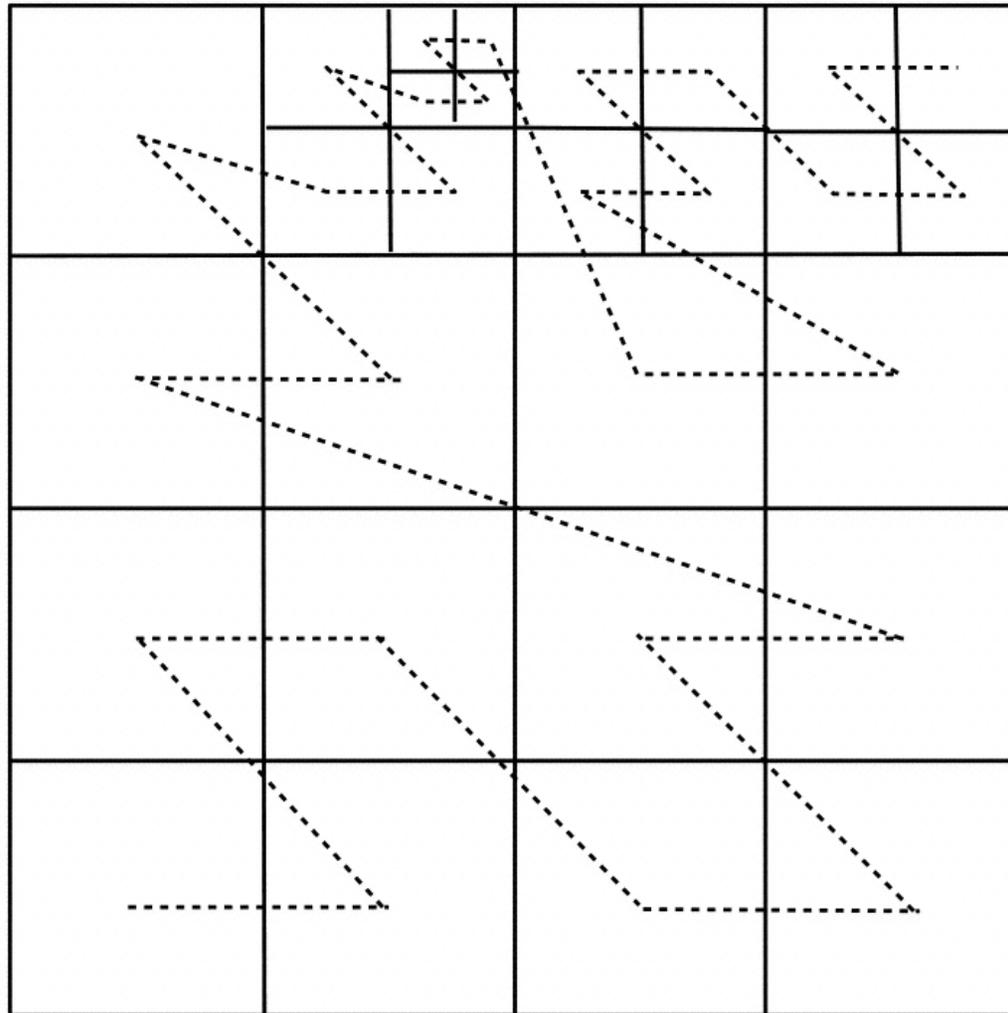
Subcycling- Zingale & Dursi  
<http://xxx.lanl.gov/abs/astro-ph/0310891>



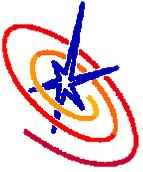
From Fryxell et al. ApJS 131 273 (2000)



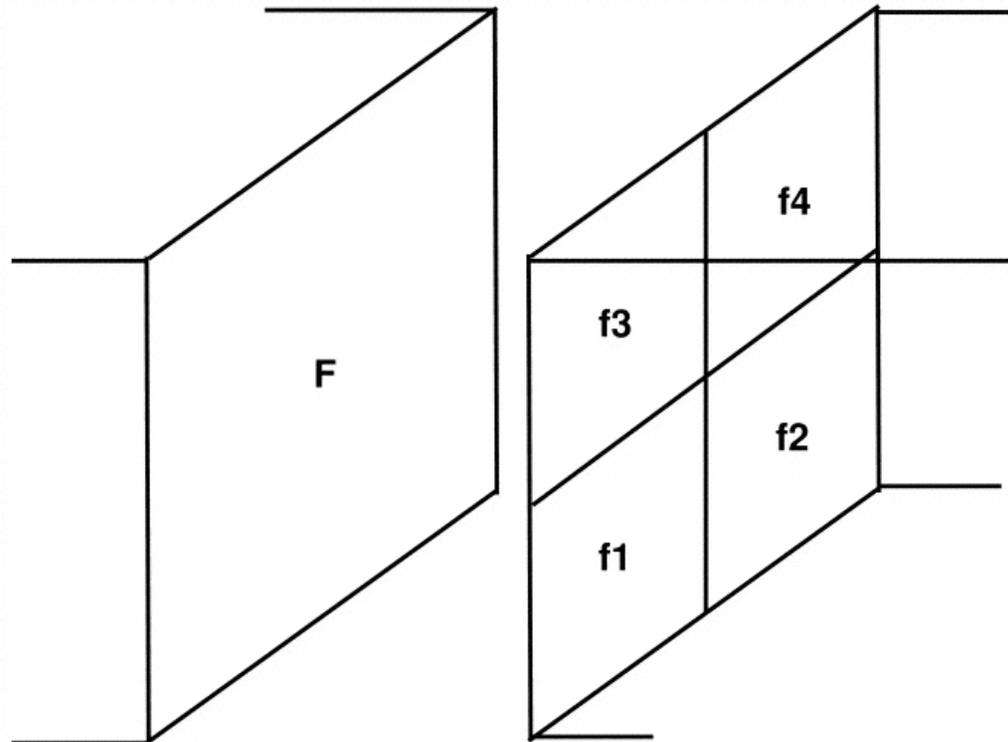
# Morton Space-filling Curve



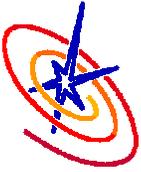
From Fryxell et al. ApJS 131 273 (2000)



# Flux Conservation at Block Boundaries



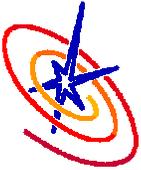
$$F = [ f1 + f2 + f3 + f4 ]$$



# Refinement Criteria

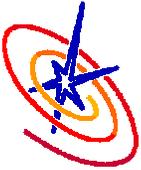
- Default is to look at the magnitude of 2<sup>nd</sup> derivative for specified quantities (e.g. density and pressure).
- As Ann mentioned, there can be sharp features (edge of star) that are not critical. One can also use locations, values of certain variables, etc.
- Best description I've heard: "black art."
- Key is to test!





# Initial Conditions

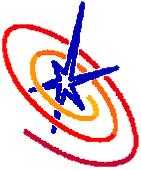
- Very important- When one constructs initial conditions, one writes a routine to initialize the blocks.
- Typical uniform mesh codes perform a loop stuffing arrays over the whole domain. Initializing a block requires querying its location and initialize the variables accordingly. **This process can be difficult to conceptualize.**
- For this Summer School, we will look at three setups relevant to simulating Type Ia supernovae
  - cellular detonation
  - 1-d deflagration
  - 2-d detonation in a white dwarf.
- Homework assignment: Modify the cellular detonation setup to instead simulate a 1-d deflagration. (Details below).



# System Requirements for Flash

---

- Compiler for Fortran (F90) and C.
- Installed copy of the Message Passing Interface (MPI)
- Installed packages for I/O, Hierarchical Data Format (HDF) or Parallel NetCDF (PnetCDF). There is a Fortran I/O option, but your mileage will vary.
- Flash is distributed with the PARAMESH AMR library included. For Chombo AMR, one must have the Chombo library included.
- For the implicit Diffuse and Hypre solvers, one must have the Hypre library installed.
- GNU make utility.
- Python 2.2 or later for the setup script.



## Running Flash II

Move into or create the run directory (usually in the scratch space)

```
mkdir 20110712_cellular  
cd 20110712_cellular
```

Copy the required files into the run directory

```
cp ../FLASH4-alpha_release/object/SpeciesList.txt .  
cp ../FLASH4-alpha_release/object/helm_table.dat .  
cp ../FLASH4-alpha_release/object/flash.par .  
cp ../FLASH4-alpha_release/object/flash4 .
```

Copy or create a run script in the run directory

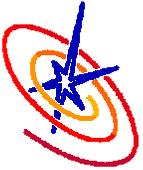
```
vi (or emacs) hopper.run (example next slide)
```

Submit the job to the queue:

```
qsub hopper.run
```

Monitor the job as you please:

```
qstat -u username
```



## Example run script for Hopper

---

Example run script:

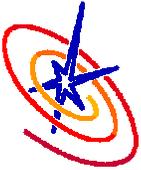
```
#PBS -N cellular01
#PBS -q debug
#PBS -l mppwidth=12
#PBS -l walltime=0:29:00
#PBS -e output.$PBS_JOBID.err
#PBS -o output.$PBS_JOBID.out

cd $PBS_O_WORKDIR

echo Starting `date`

aprun -n 12 ./flash4

echo Ending `date`
```



# Operator Splitting

The different modules operating on the state are strung together via Strang splitting, a fractional step method, in which the operators act on parts of one time step.

Consider advection + reaction:

$$\text{Problem A: } q_t + uq_x = 0$$

$$\text{Problem B: } q_t = -\lambda q$$

Want to solve combined problem:

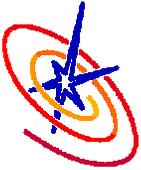
$$q_t = (A + B)q \quad \text{where } A = -u\partial_x \text{ and } B = \lambda(x)$$

Solve via

$$q_t = Aq \quad \Delta t/2$$

$$q_t = Bq \quad \Delta t$$

$$q_t = Aq \quad \Delta t/2$$



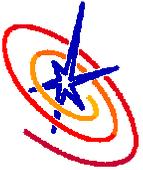
## Driver Routine Illustrating Strang Splitting

```
do dr_nstep = dr_nbegin, dr_nend

  call Hydro( blockCount, blockList, &
             dr_simTime, dr_dt, dr_dtOld, dr_fSweepDir)
  call RadTrans(blockCount, blockList, dr_dt, pass=1)
  call Diffuse(blockCount, blockList, dr_dt, pass=1)
  call Driver_sourceTerms(blockCount, blockList, dr_dt, pass=1)
  call ravity_potentialListOfBlocks(blockCount,blockList)

  call Hydro( blockCount, blockList, &
             dr_simTime, dr_dt, dr_dtOld, dr_rSweepDir)
  call RadTrans(blockCount, blockList, dr_dt, pass=2)
  call Diffuse(blockCount, blockList, dr_dt, pass=2)
  call Driver_sourceTerms(blockCount, blockList, dr_dt)
  call Gravity_potentialListOfBlocks(blockCount,blockList)

end do
```



Euler equations :

$$\frac{\partial \mathbf{U}}{\partial t} + \nabla \cdot \mathbf{F}(\mathbf{U}) = \mathbf{S}(\mathbf{U}) ,$$

Conserved quantities:  $\mathbf{U} = (\rho, \rho v, \rho E)^T$

Volume average

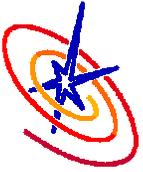
$$\frac{1}{V} \int \left\{ \frac{\partial \mathbf{U}}{\partial t} + \nabla \cdot \mathbf{F}(\mathbf{U}) \right\} dV = \frac{1}{V} \int \mathbf{S}(\mathbf{U}) dV$$

$V$  Volume

take  $\langle \mathbf{U} \rangle$  as volume average of  $\mathbf{U}$

Integral form of Euler equations :

$$\frac{\partial \langle \mathbf{U} \rangle}{\partial t} + \frac{1}{V} \oint \mathbf{F}(\mathbf{U}) \mathbf{n} \cdot d\mathbf{S} = \langle \mathbf{S}(\mathbf{U}) \rangle .$$



# Finite Volume Methods

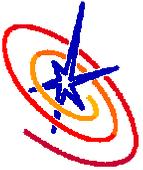
In finite volume methods, the average value of the unknown is given by

$$\langle f \rangle_i = \frac{1}{\Delta x} \int_{x_{i-1/2}}^{x_{i+1/2}} f(x) dx$$

Where  $x_{i+1/2}$ ,  $x_{i-1/2}$  are the positions of the left, right edges of the zone.

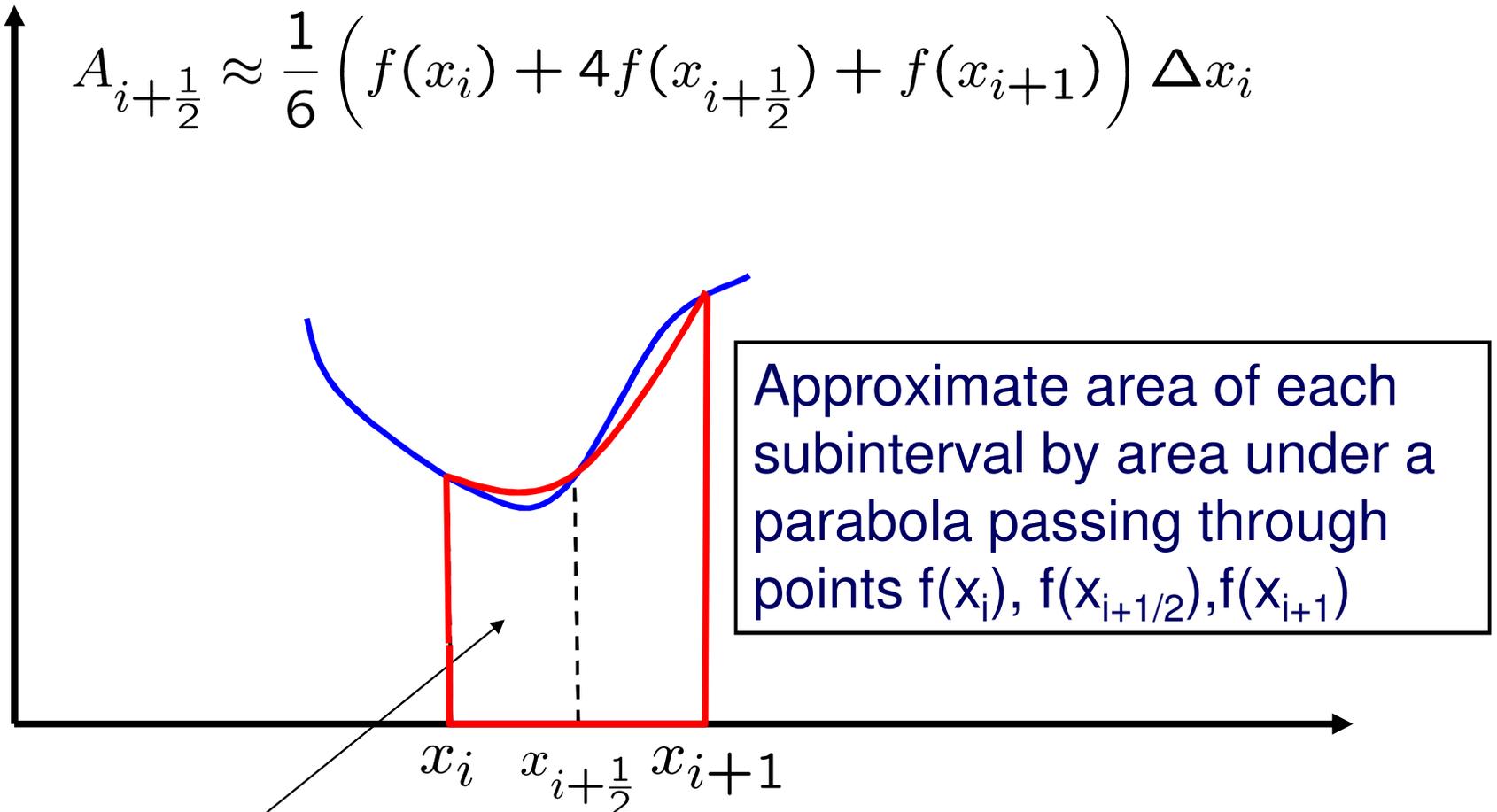
One performs a reconstruction (piecewise constant, linear, parabolic, ...) to get  $f(x)$  and then one integrates that.

Parabolic example is Simpson's rule (seen for integration)

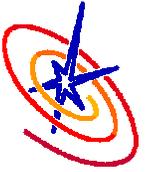


# Simpson's Rule

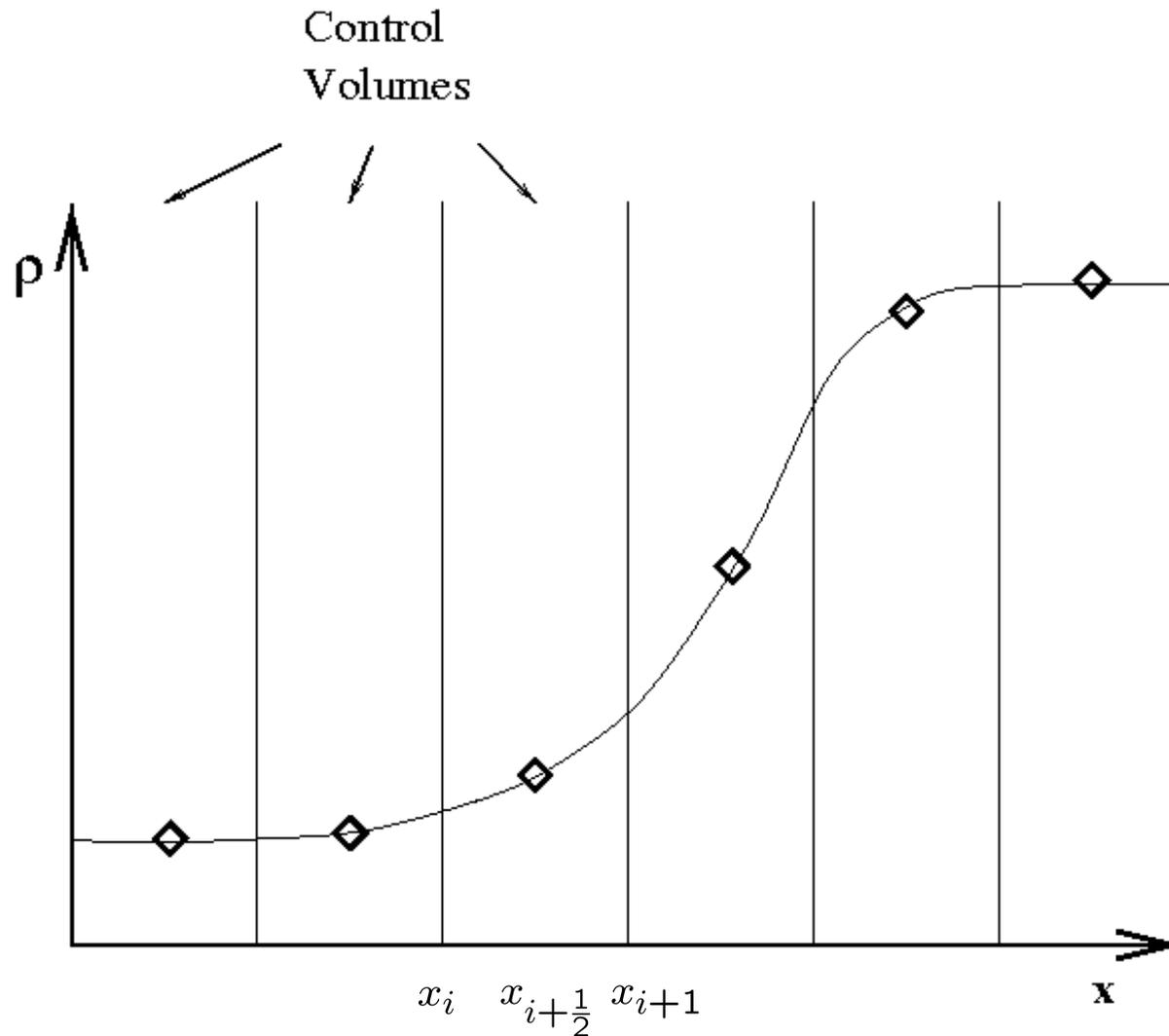
$$A_{i+\frac{1}{2}} \approx \frac{1}{6} \left( f(x_i) + 4f(x_{i+\frac{1}{2}}) + f(x_{i+1}) \right) \Delta x_i$$



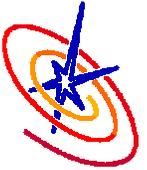
$$A_{i+\frac{1}{2}} = \text{Area of } i+1/2\text{th subinterval}$$



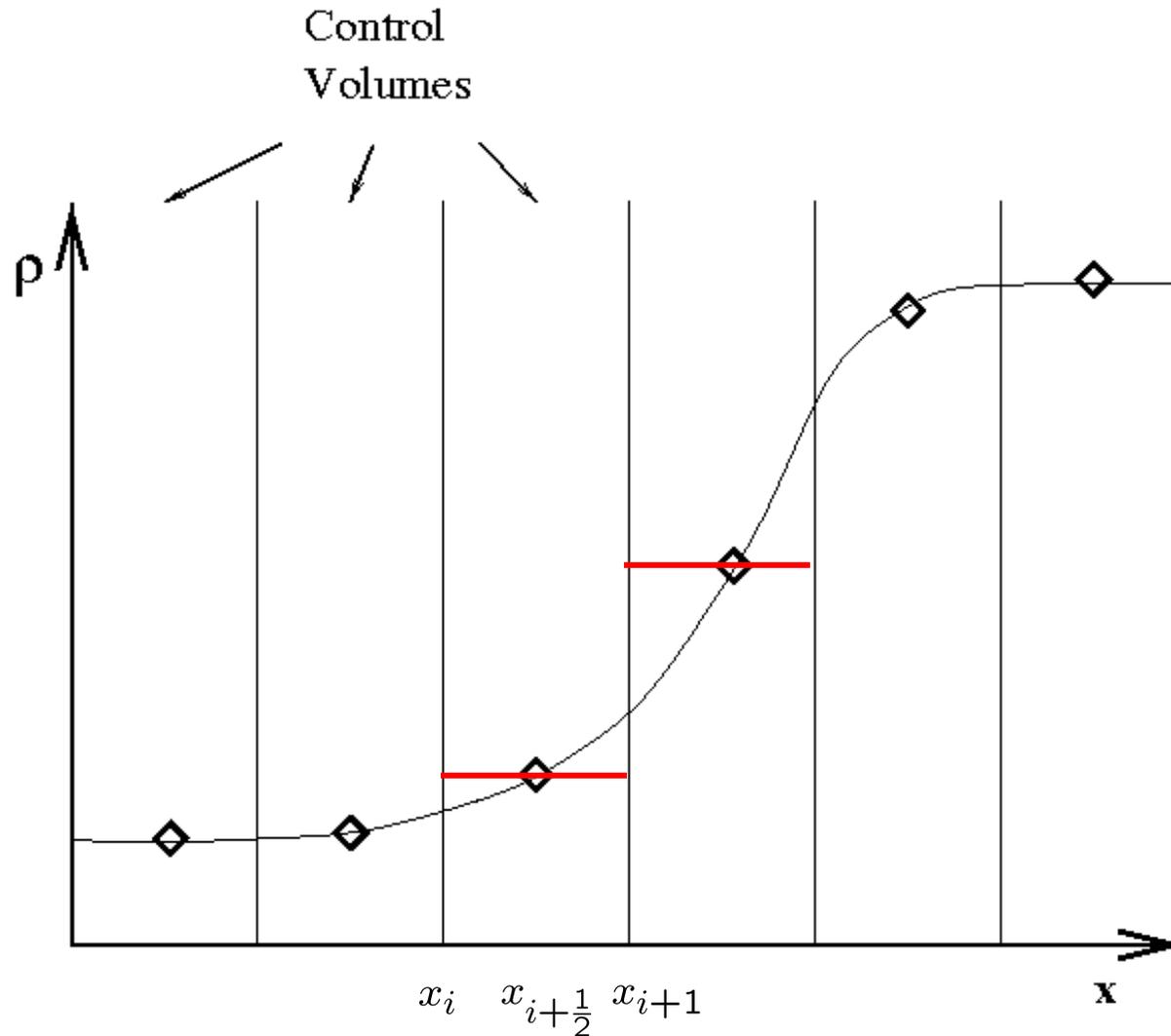
# Finite Volume Hydrodynamics Methods



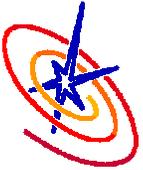
Divide the domain into zones the interact with fluxes



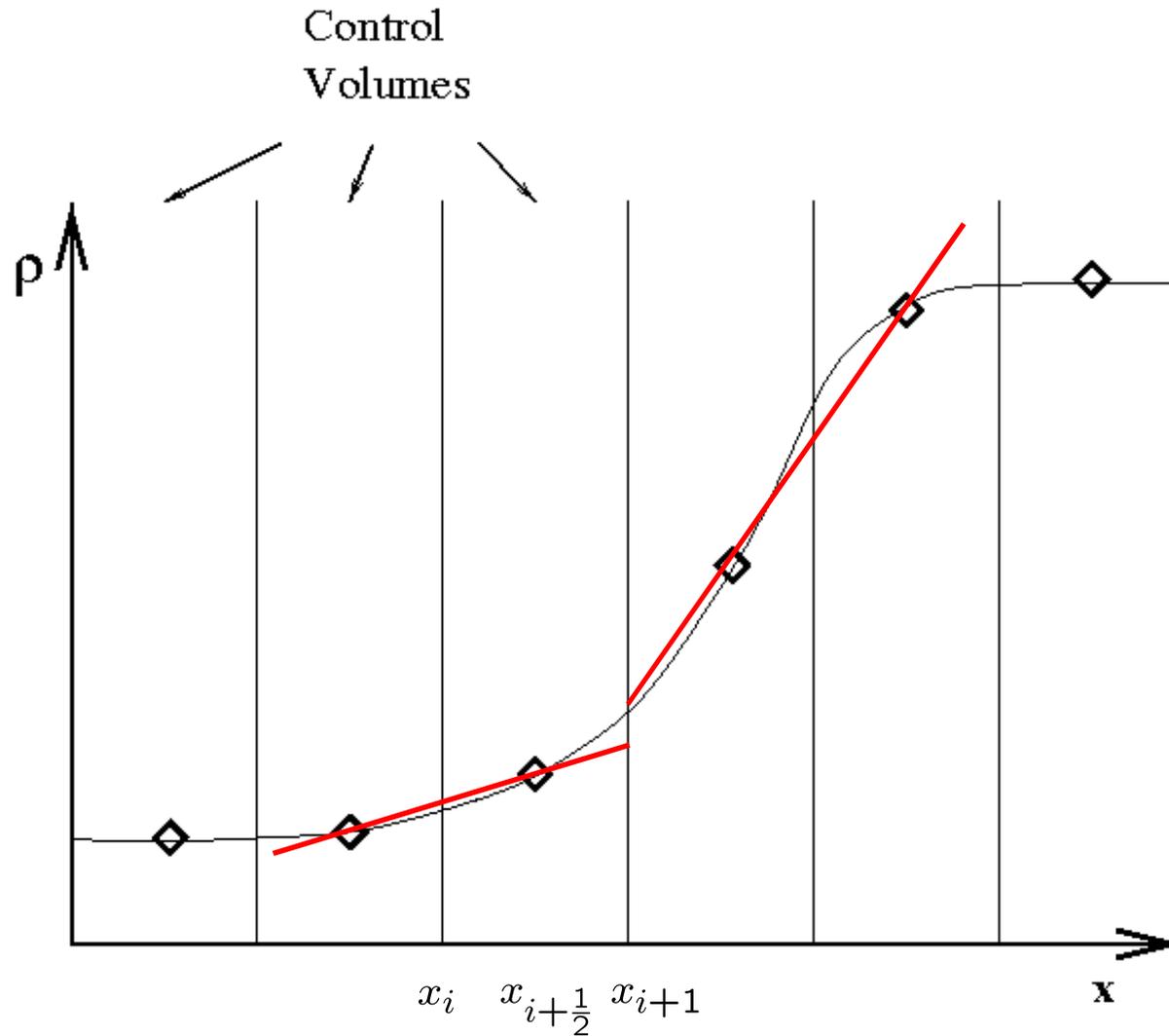
# Godunov Method



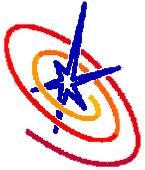
The original Godunov method solved the Riemann problem at the boundaries between zones using the average values



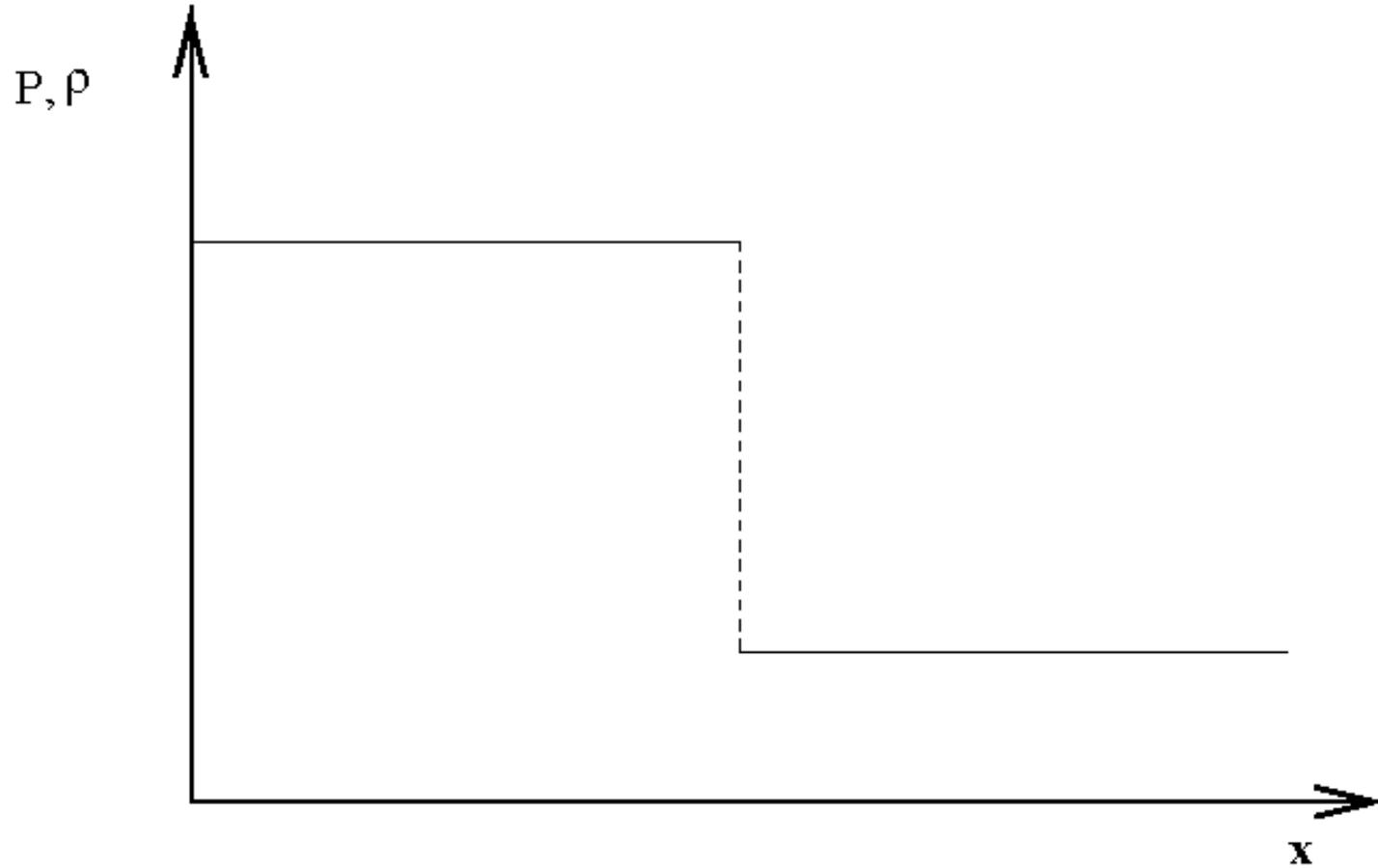
# Piecewise Linear Godunov Methods



Piecewise linear methods perform a linear interpolation.  
Higher-order methods exist. PPM is Piecewise-Parabolic Method



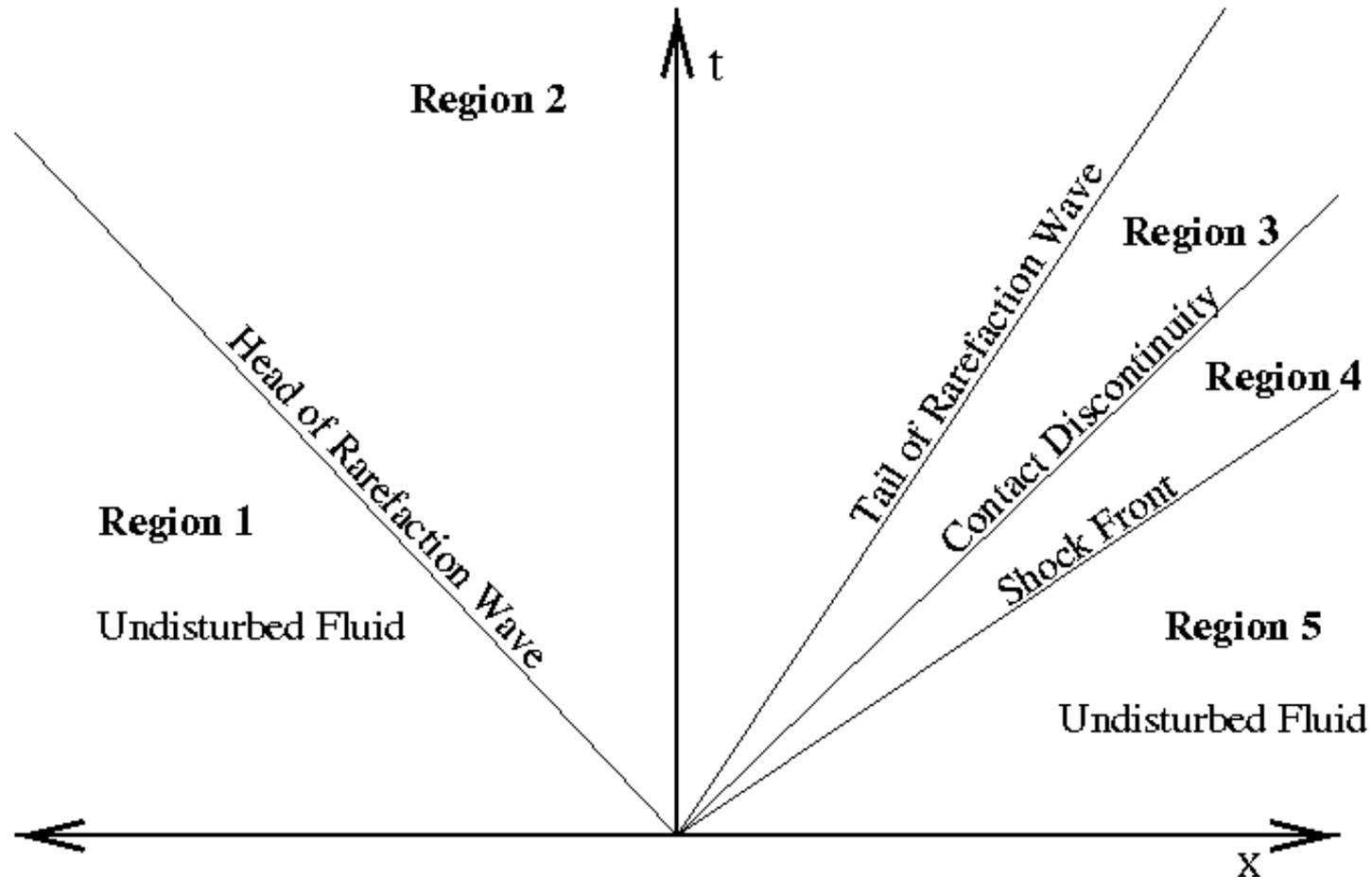
# Riemann Problem: Shock Tube



Initial conditions: a discontinuity in density and pressure



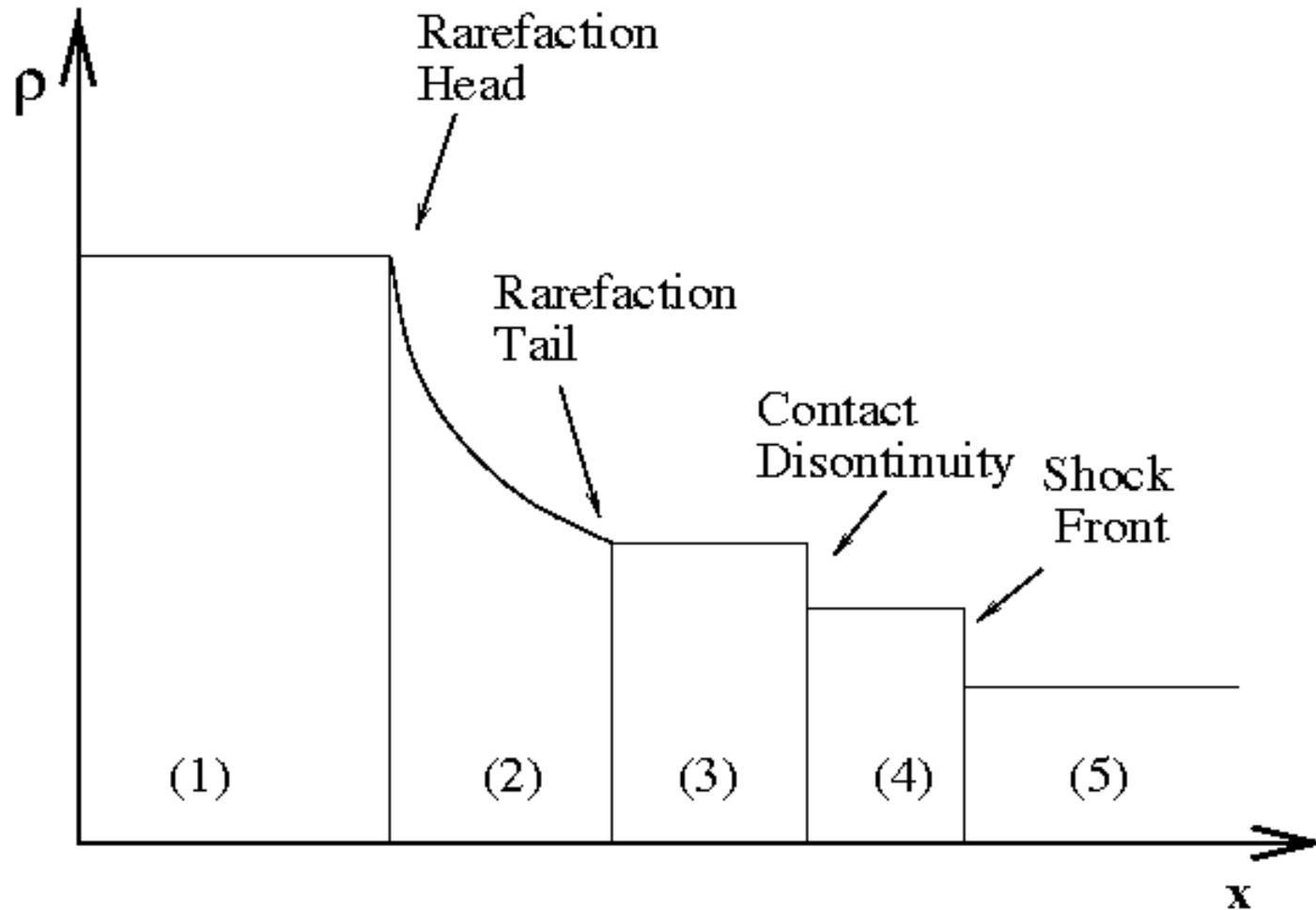
# Riemann Problem: Shock Tube



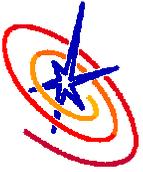
World diagram for Riemann problem



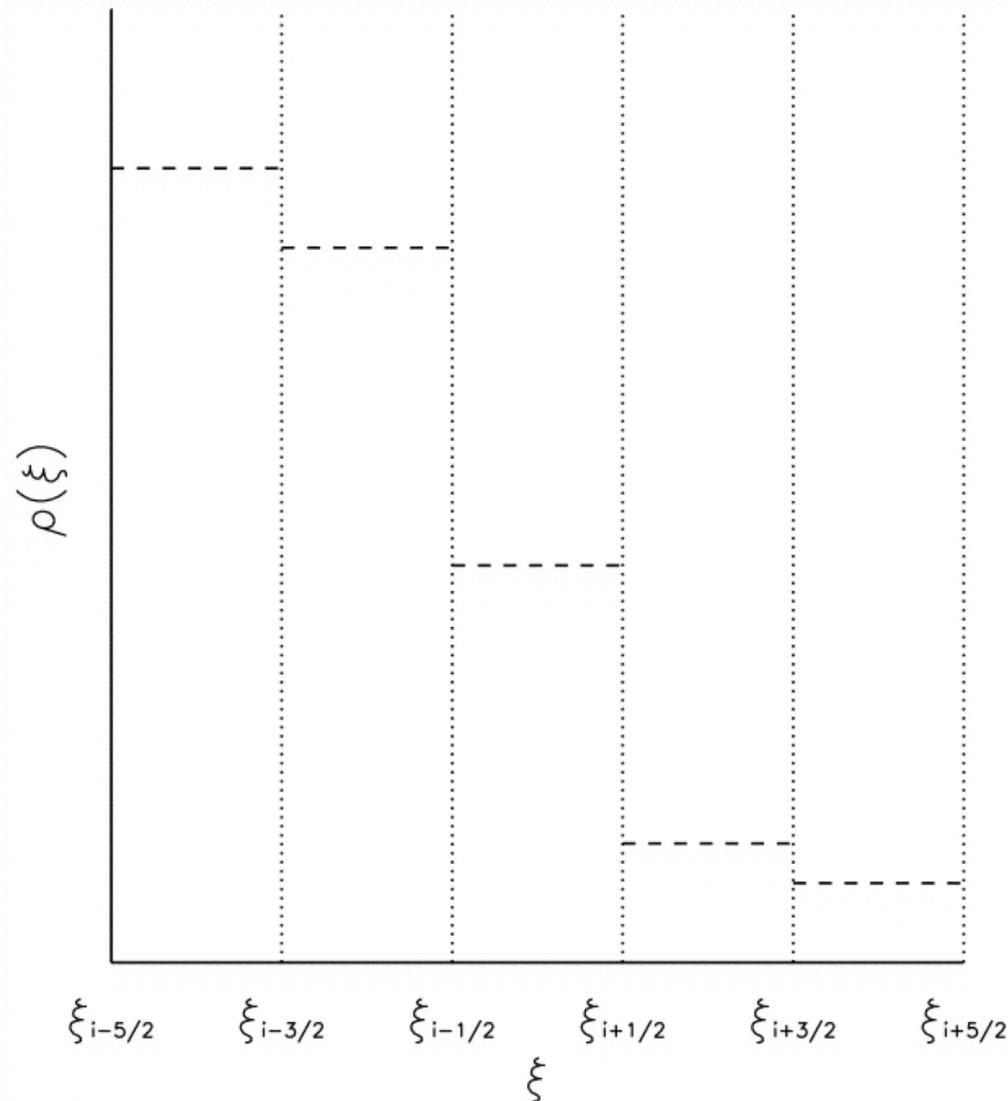
# Riemann Problem: Shock Tube



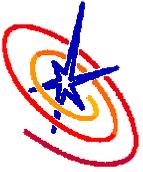
PPM has special algorithms for these features



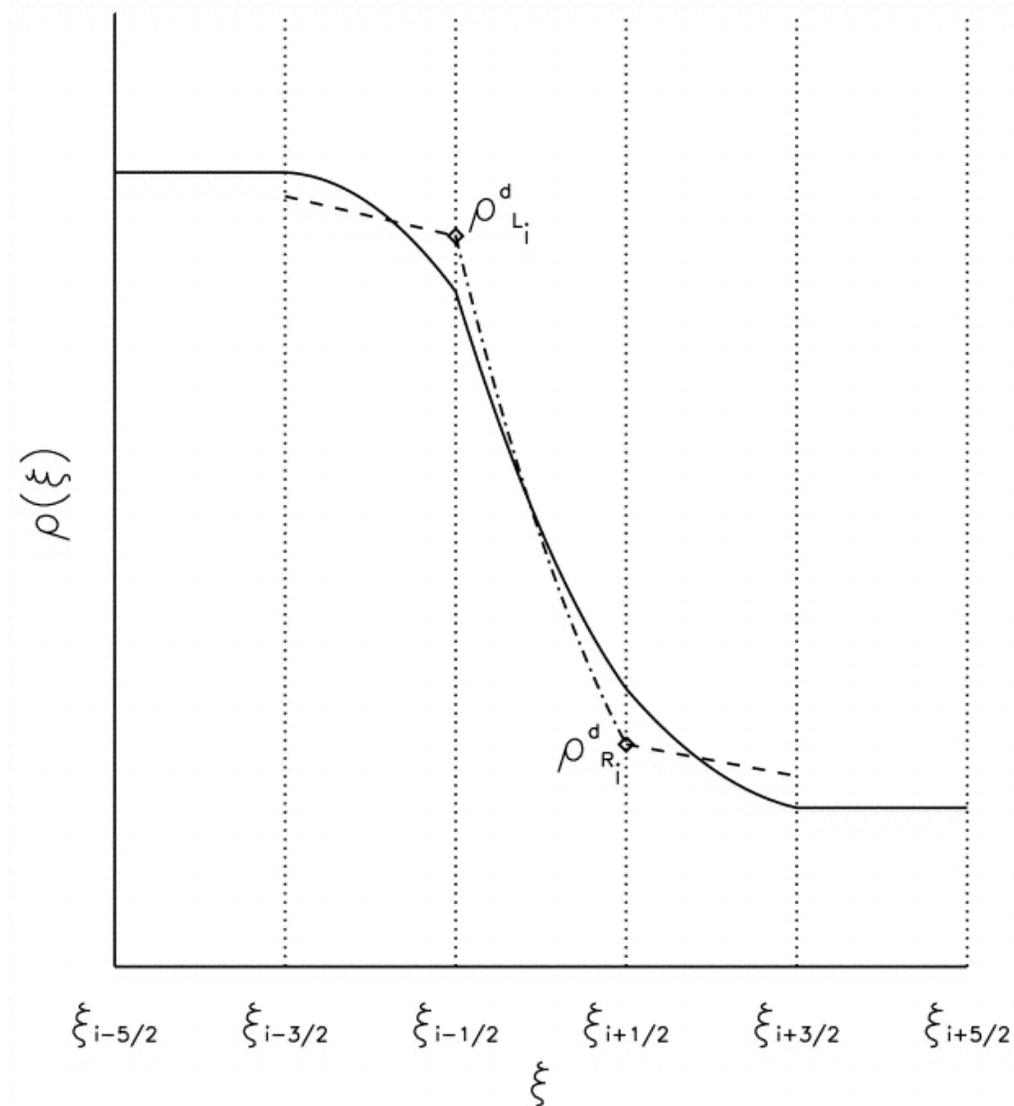
# Contact Discontinuity Detection

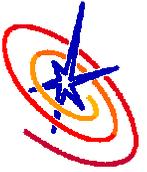


Density profile  
that will trigger  
special algorithm

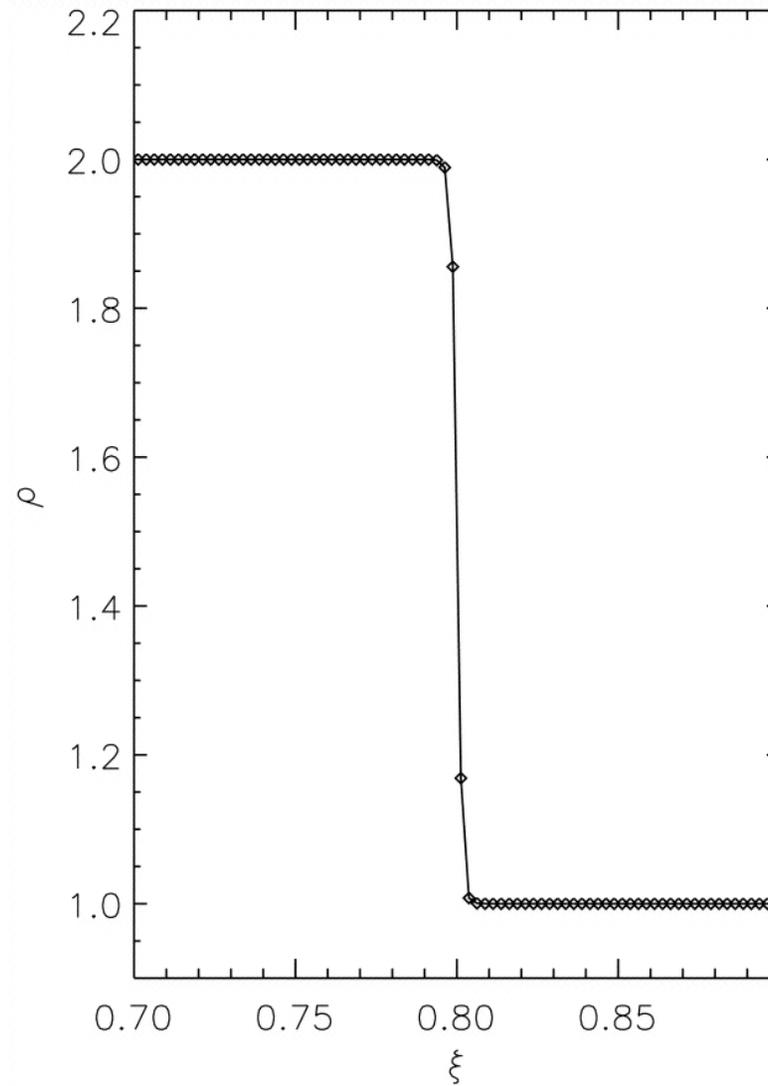


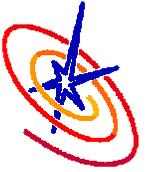
# Contact Steepening Process



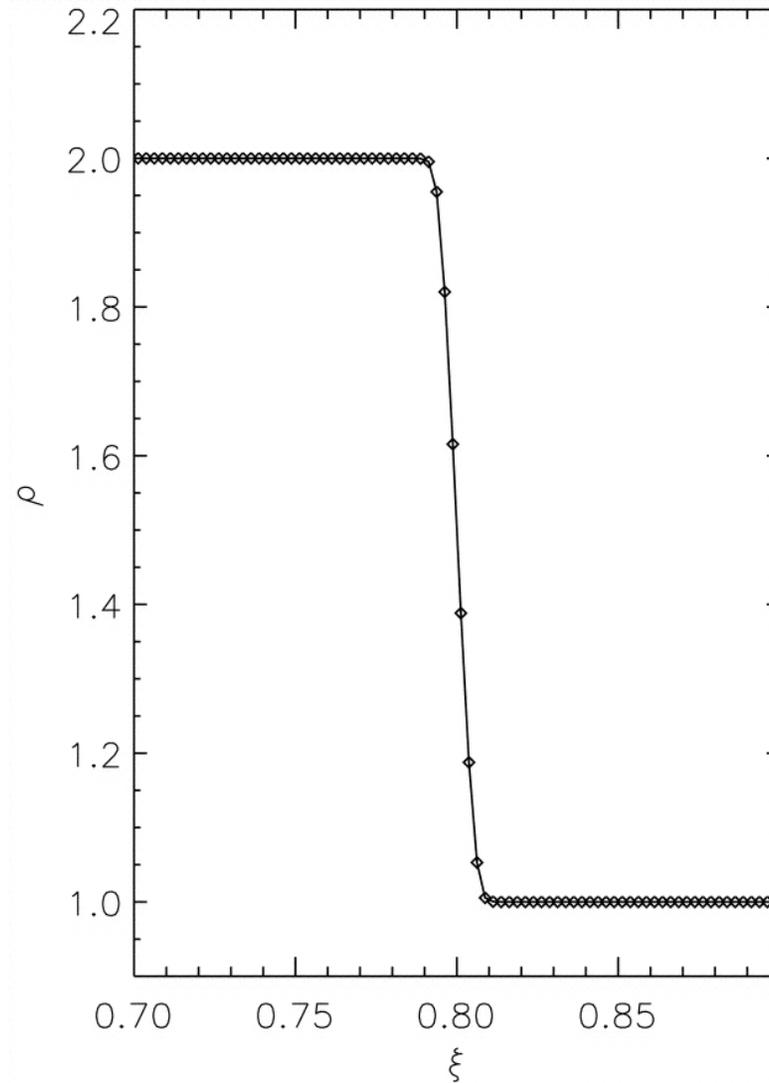


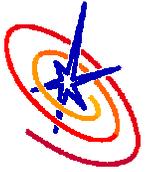
# Contact Discontinuity w/ steepening





# Contact Discontinuity w/o steepening





# Intermission

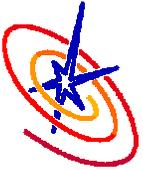




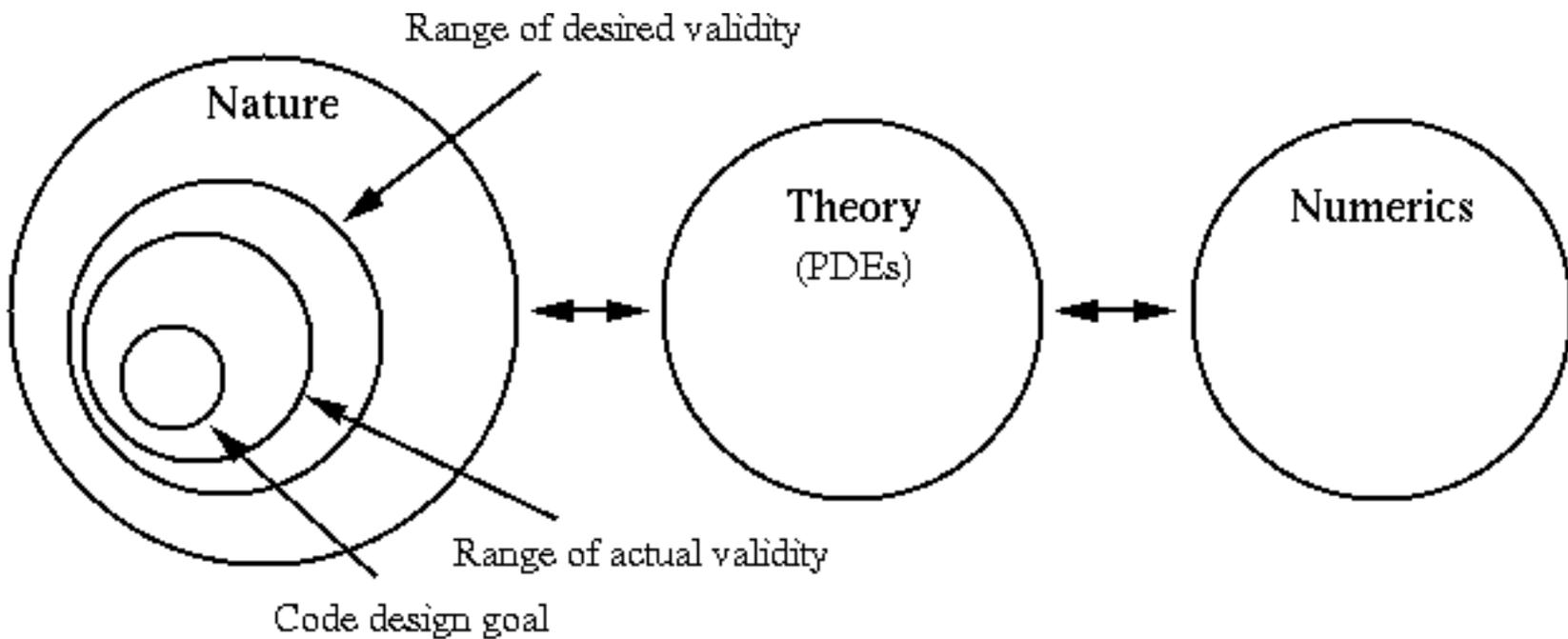
# V&V Vocabulary

---

- Verification- Determining that the implementation accurately represents the conceptual description of the model.
  - Quantify error.
  - Approach is a systematic refinement study (space and time).
  
- Validation- Determining the degree to which a model is an accurate representation of the real world.
  - Test key elements (modules) and integrated code.
  - Compare to actual experiments (quantify error).
  
- Calibration- process performed to improve the agreement between simulation and experiment. Not validation!
  
- Prediction- use of the code or model for an application for which it has not been validated.

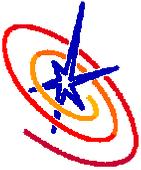


# Verification and Validation



Verification: “solving the equations right”

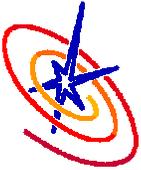
Validation: “solving the right equations”



# Our V&V Methodology

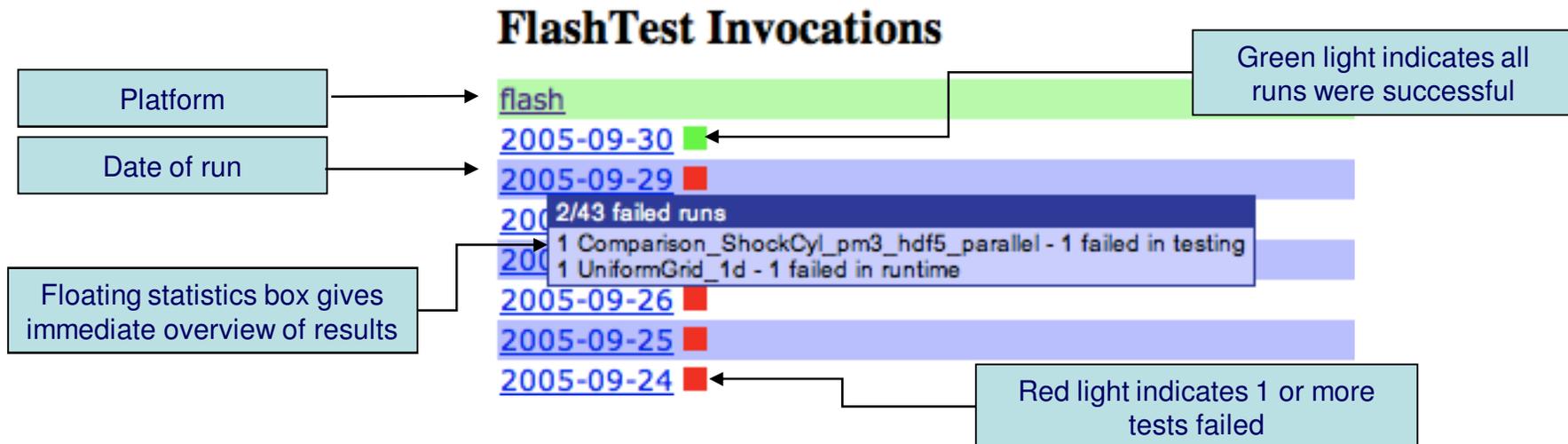
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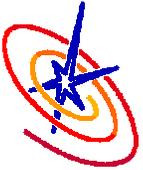
- Choose V&V tests/problems for particular code modules e.g. hydrodynamics. Test integrated code also if possible.
  
- Verification test problems
  - Unit tests
  - Investigate convergence of error with resolution
  - Investigate error in secondary modules e.g. EOS
  - Regularly re-verify with nightly/weekly automated tests
  
- Validation problems
  - Quantify measurements in experiment and simulation
  - Quantify error and uncertainty in experiment and simulation
  - Resolution study (verification-type tests)
  
- Note: astrophysics is largely prediction.



# Verifiability: The New Test Suite

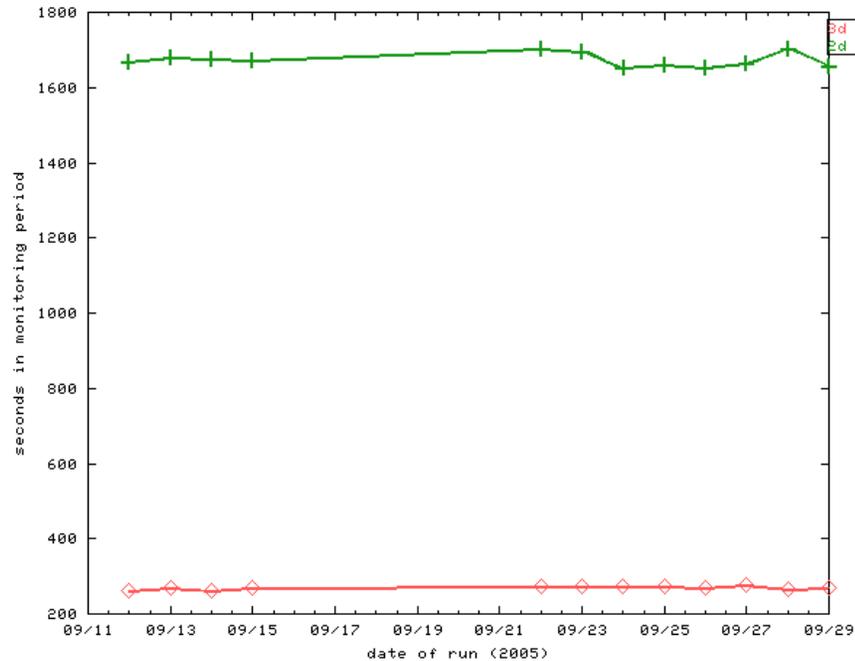
- Flash test suite automatically runs set of verification tests
- Essential for identifying bugs unintentionally introduced
- New test suite released with FLASH3 so users can monitor their own research problems and performance
  - test parameters easily modified through GUI
  - handles unit tests, compilation tests, comparison tests
  - automatically uploads test suite data to benchmarks database



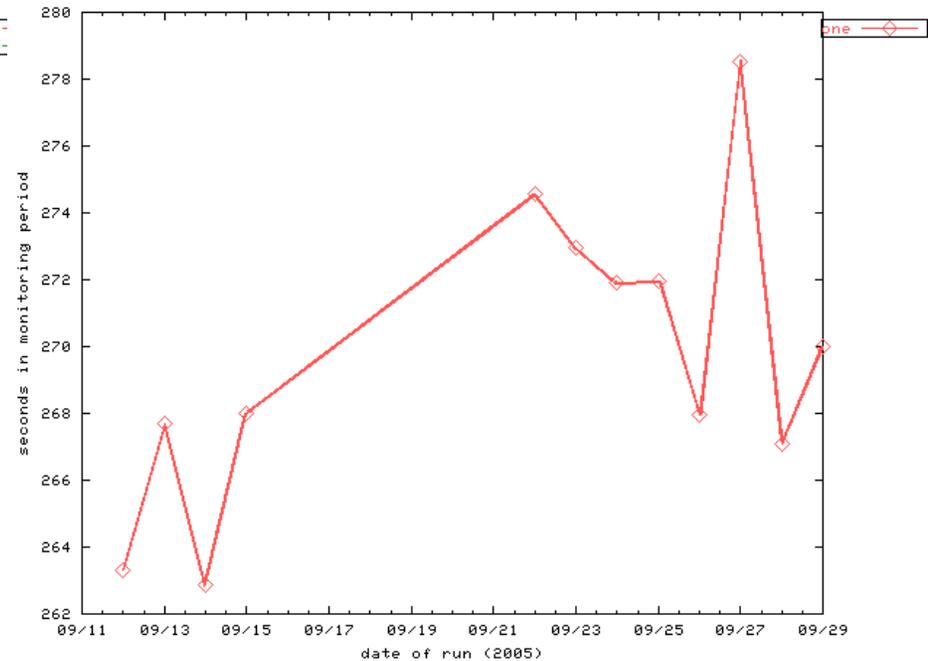


# Test Suite Performance History

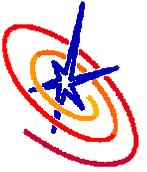
## History of 2D and 3D Sedov Problems



## Details of 2D History

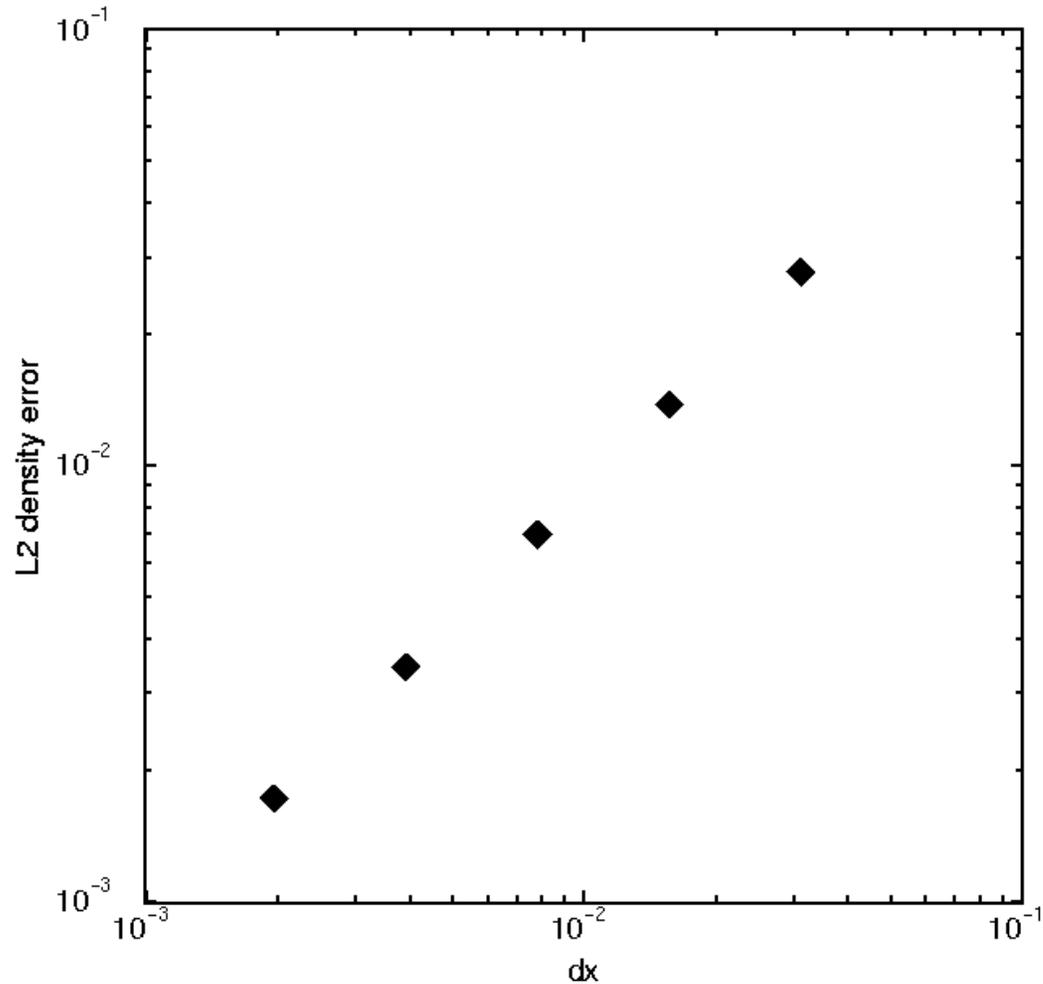


*The test suite adds the ability to upload selected test log files to the database to track daily code performance.*

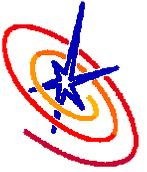


# Verification Test: Sod Shock Tube

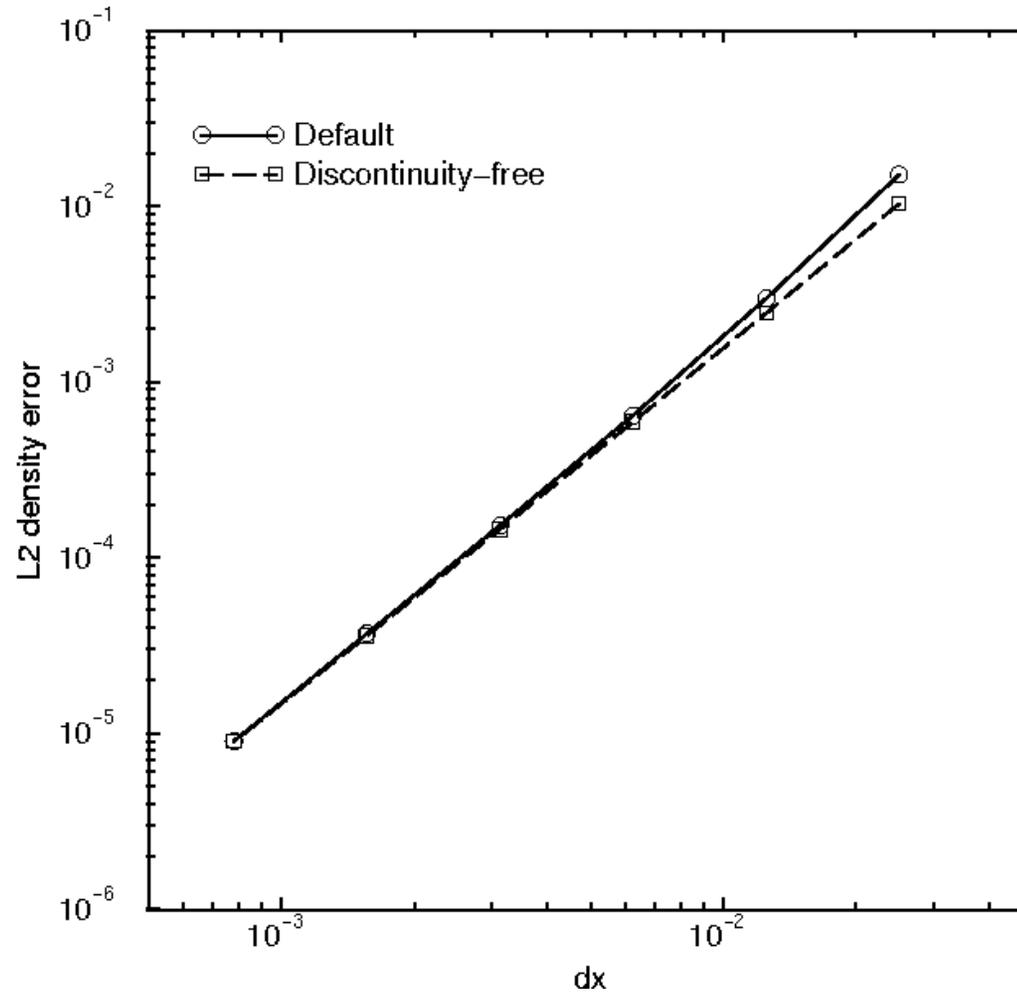
$$L_2 = \left[ \frac{\sum (|\phi - \phi_a|)^2}{\sum (\phi_a)^2} \right]^{\frac{1}{2}}$$



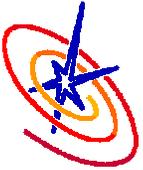
Demonstrates expected 1<sup>st</sup> order convergence of error



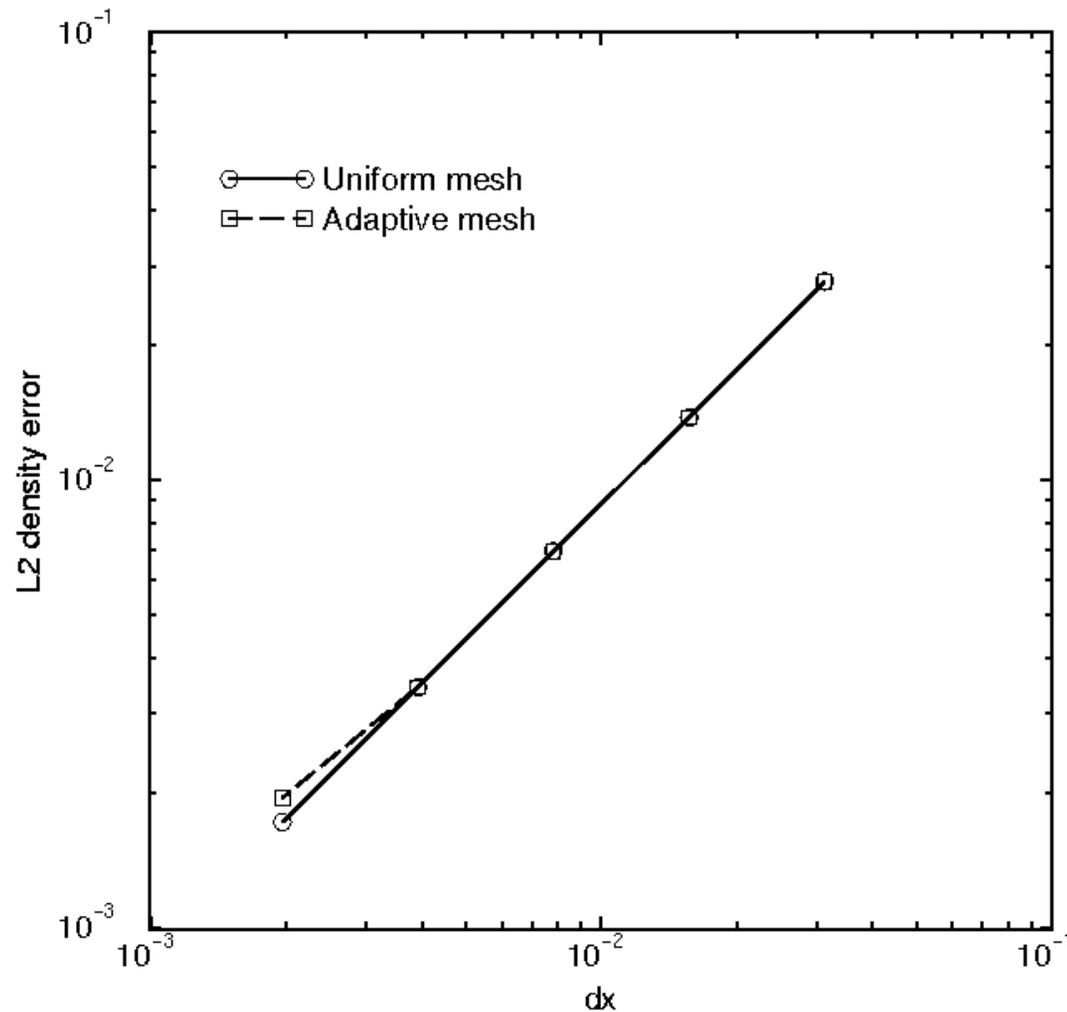
# Verification Test: Isentropic Vortex



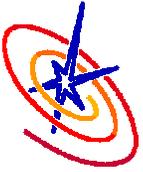
Demonstrates expected 2<sup>nd</sup> order convergence of error, but....



# Sod Tube W/ AMR

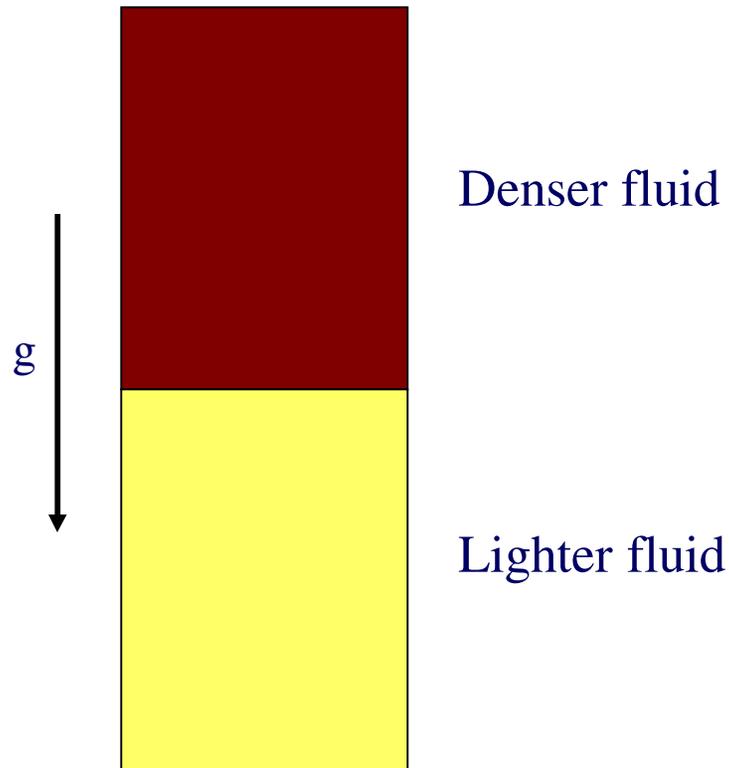


Demonstrates expected 1<sup>st</sup> order convergence of error, but note that **the imperfect mesh refinement criteria degrades the solution!**

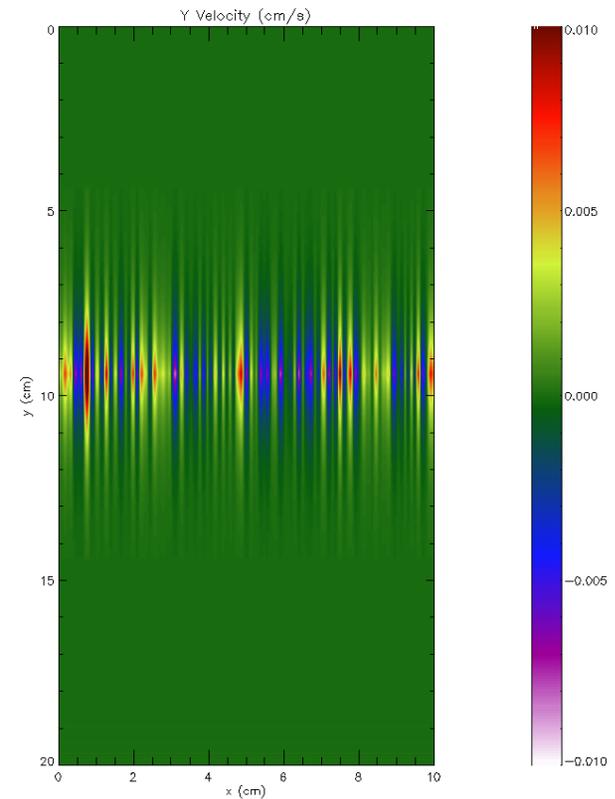


# Rayleigh-Taylor Instabilities

Density schematic:

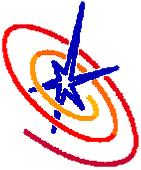


Multi-mode velocity perturbation:



time = 0.000 ps  
number of blocks = 1450  
AMR levels = 6

2.5-5 % sound speed with highest  
magnitude near the interface

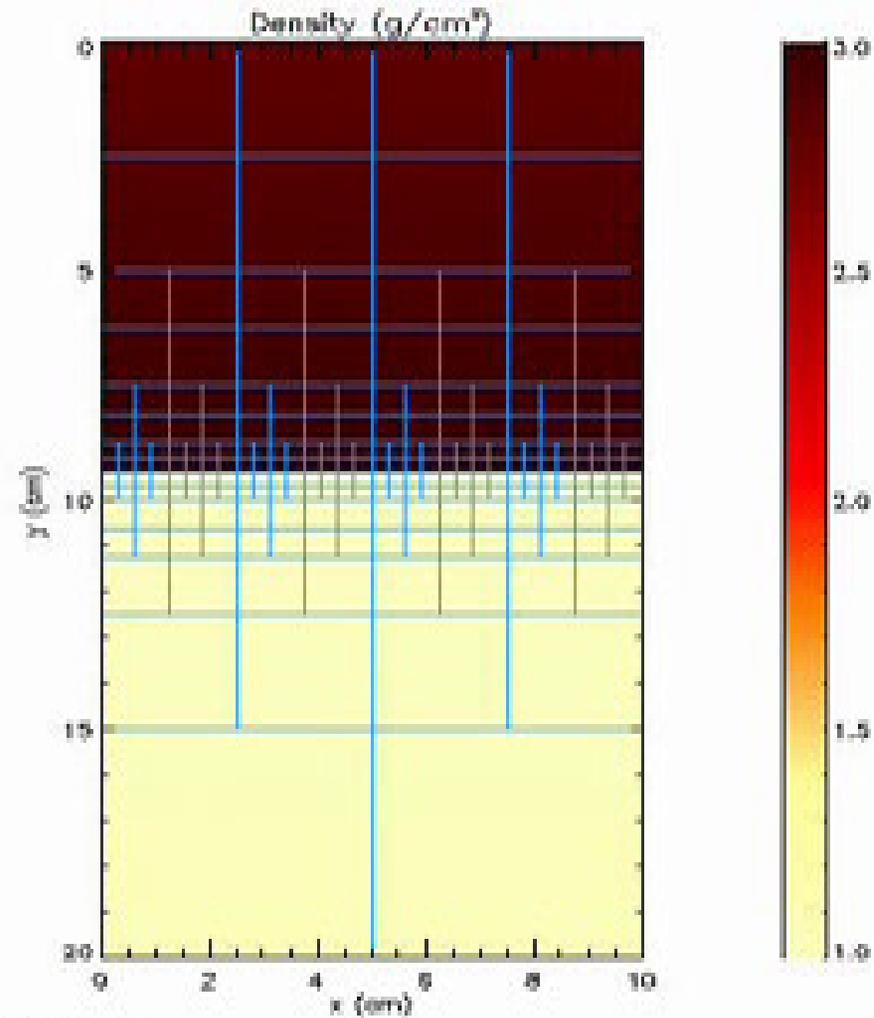


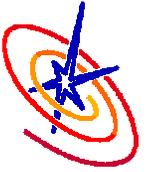
## “ $\alpha$ -Group” Consortium

- Organized by G. Dimonte (Oct. 1998)
  - Purpose – to determine if the  $t^2$  scaling law holds for the growth of the RT mixing layer, and if so, to determine the value of  $\alpha$ 
    - simulation - experiment comparisons
    - inter-simulation comparisons
- $$h_{b,s} = \alpha_{b,s} g A t^2, \text{ where } A = (\rho_2 - \rho_1) / (\rho_2 + \rho_1)$$
- Definition of standard problem set (D. Youngs)
  - Dimonte et al. Phys. Fluids **16** 1668 (2004)

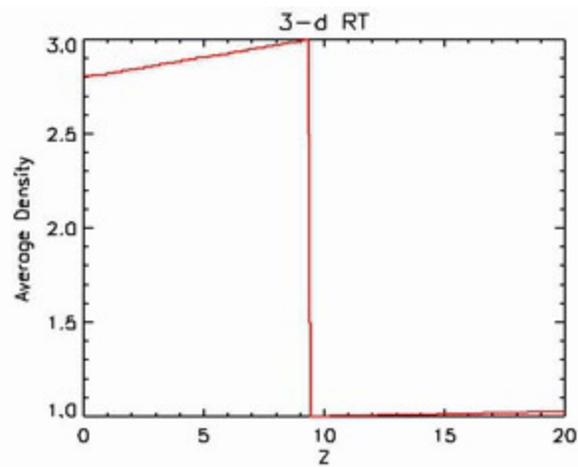


# Multi-mode Rayleigh-Taylor: 2-d Simulation

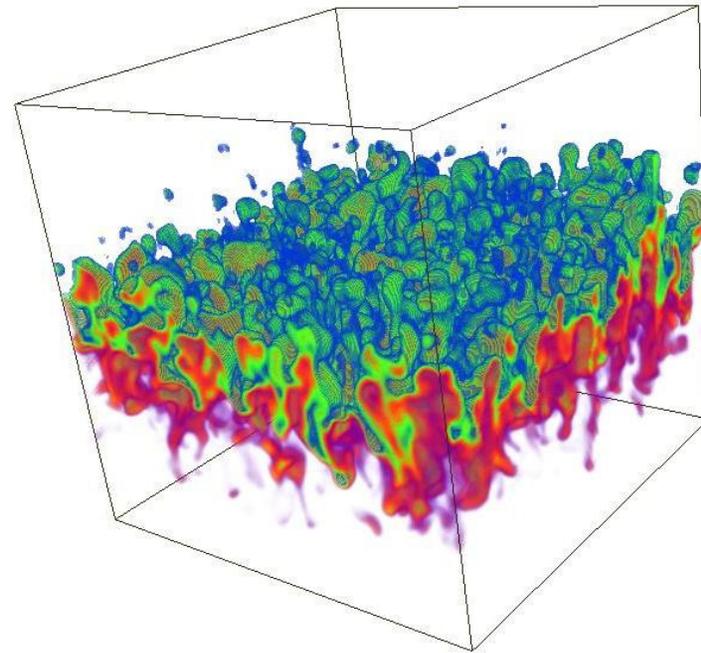




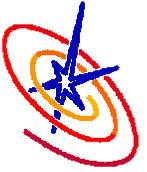
# Multi-mode Rayleigh-Taylor: 3-d Simulation



Horizontally Averaged Density

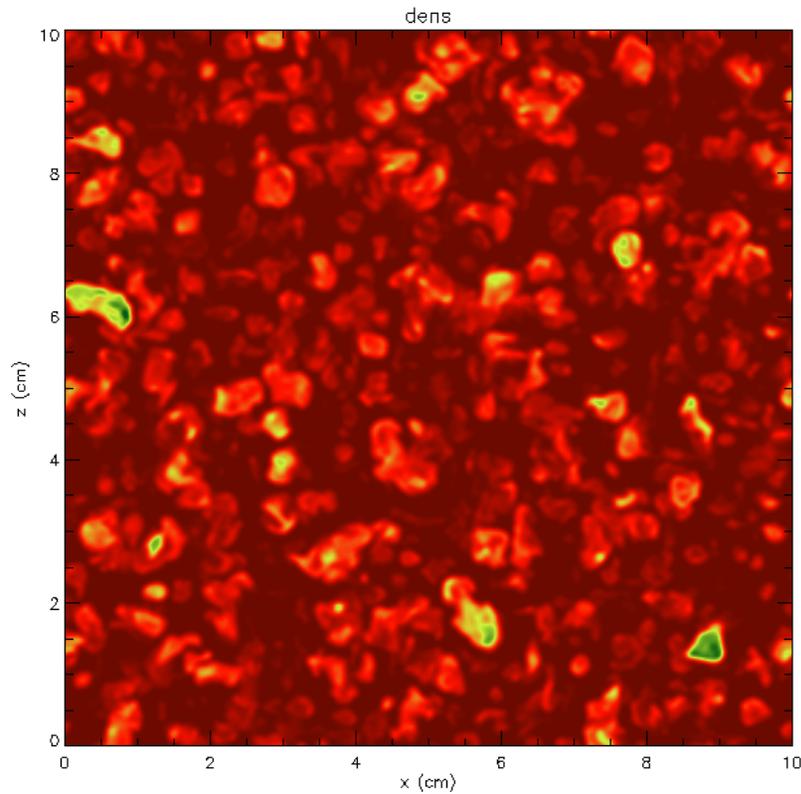


Modes 32-64 perturbed

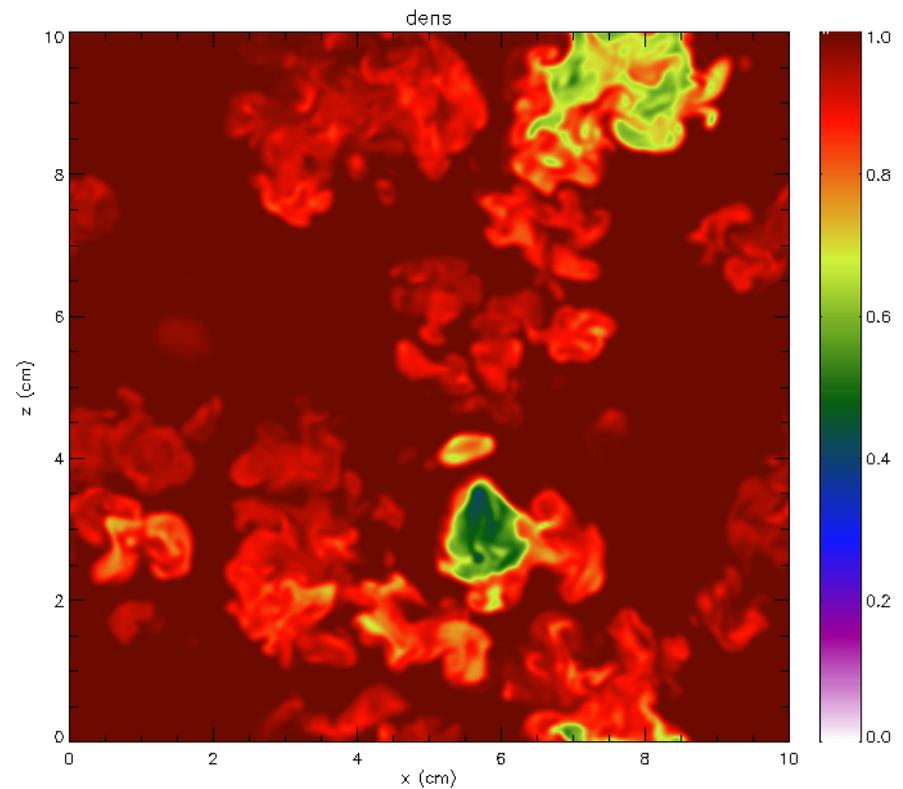


# Multi-mode Rayleigh-Taylor: Inverse Cascade

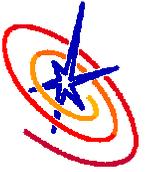
Bubbles of the lighter fluid in the denser fluid



$t = 7.00$  sec

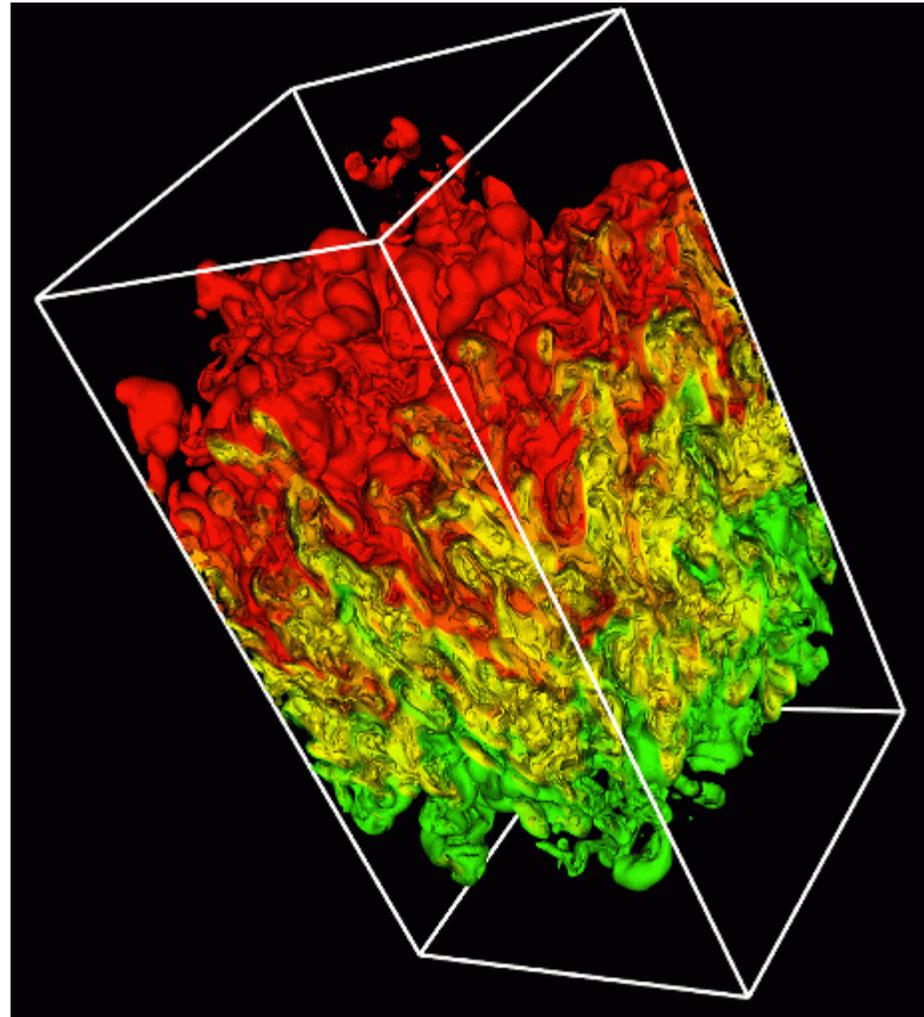


$t = 14.75$  sec



# Multi-mode Rayleigh-Taylor

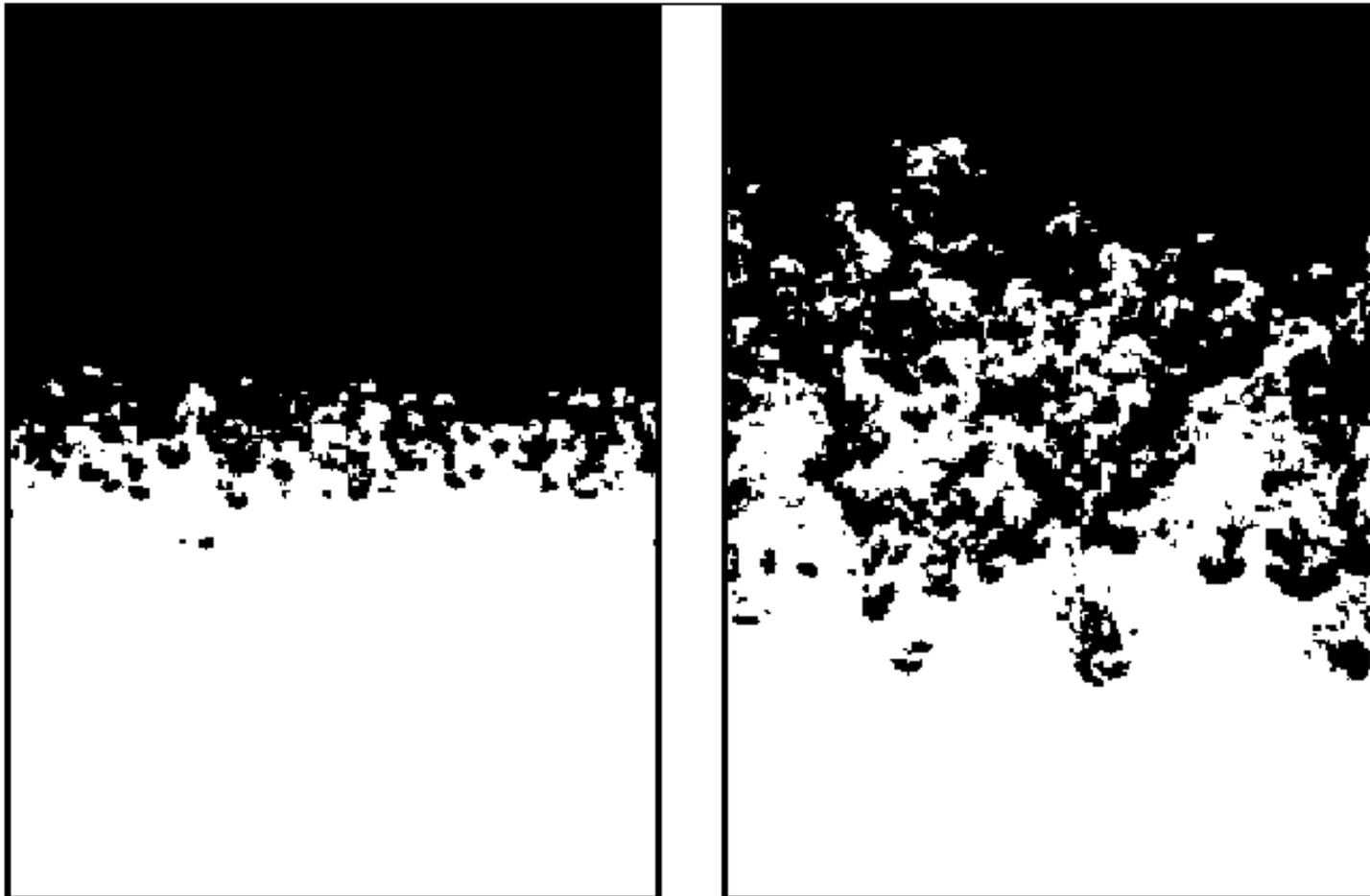
Rendering of  
Mixing Zone



Density ( $\text{g/cm}^3$ ) at  $t = 14.75$  sec



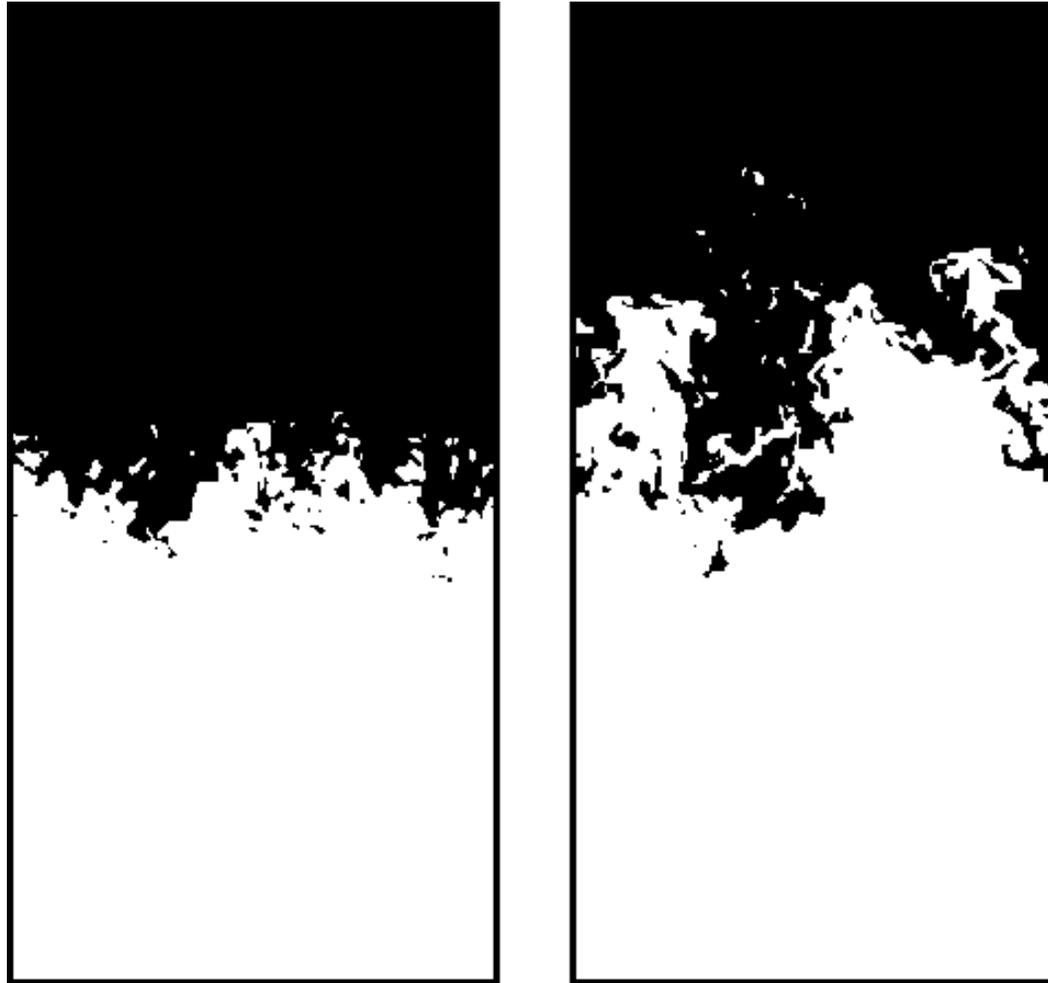
## Multi-mode R-T Experimental LIF Image



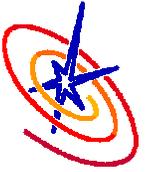
It looks similar to the simulation.....



## Multi-mode R-T Simulated LIF Image

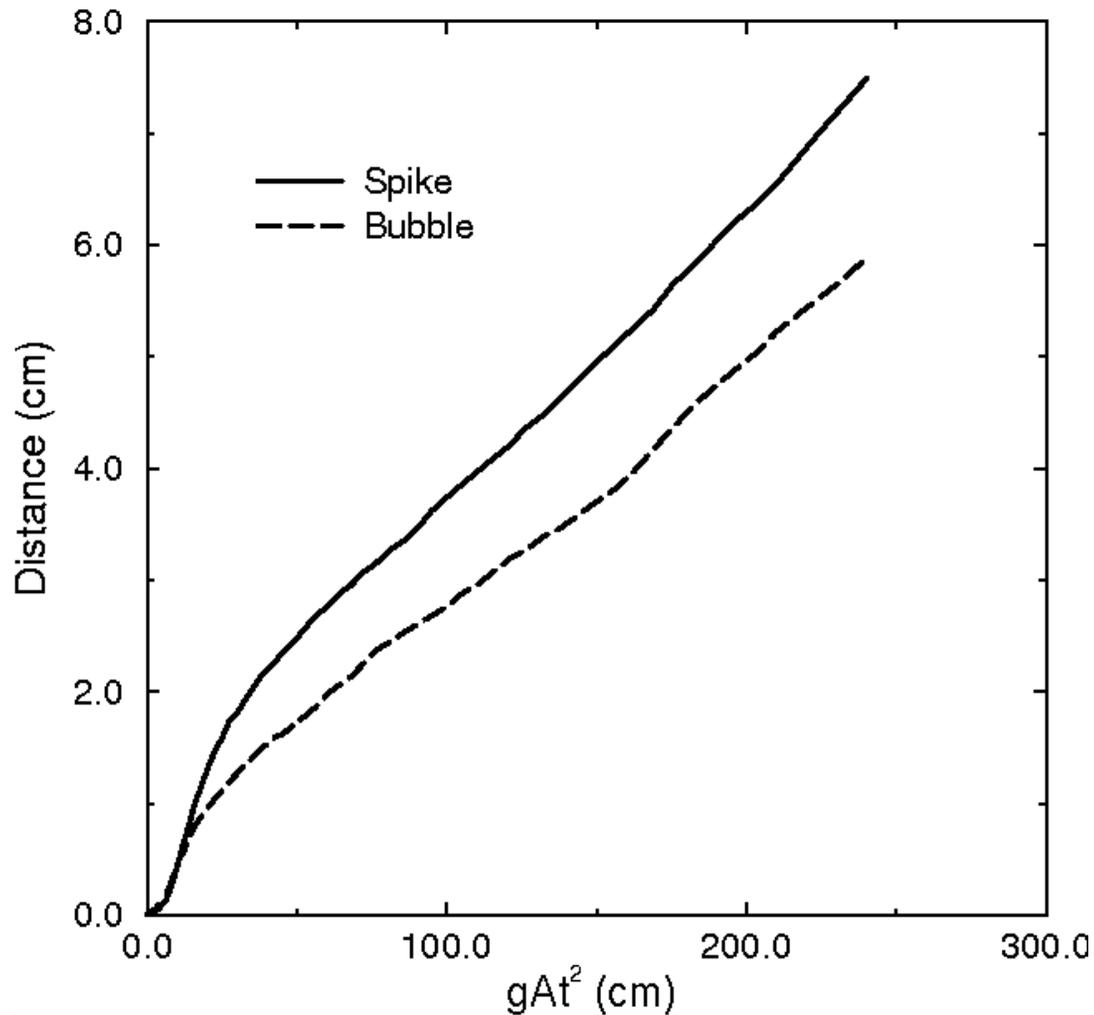


It looks similar to the experiment.....



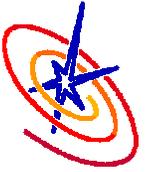
# Multi-mode Rayleigh-Taylor

FLASH Simulation



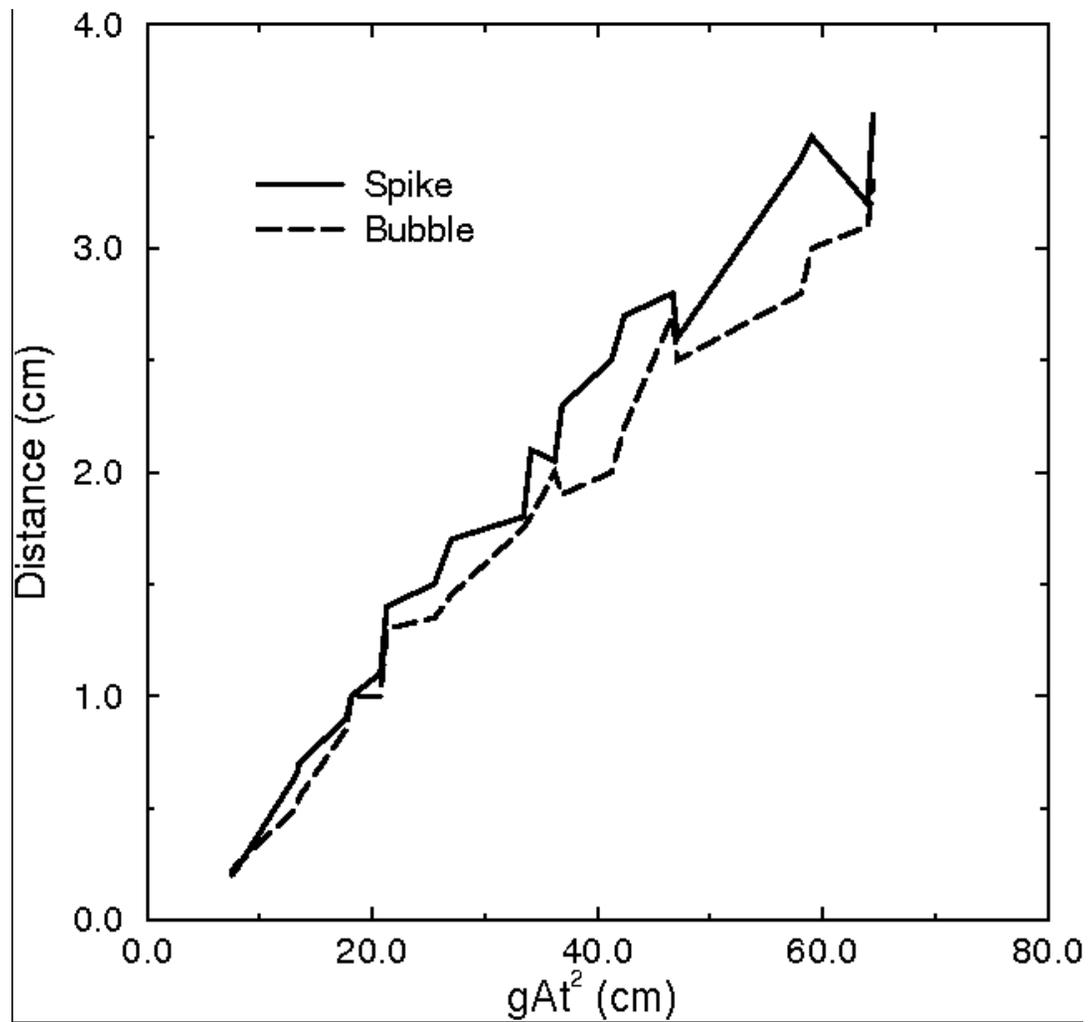
$$\alpha_{\text{spike}} = 0.026$$

$$\alpha_{\text{bubble}} = 0.021$$



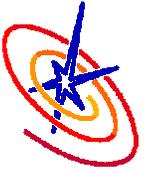
# Multi-mode Rayleigh-Taylor

## Experiment

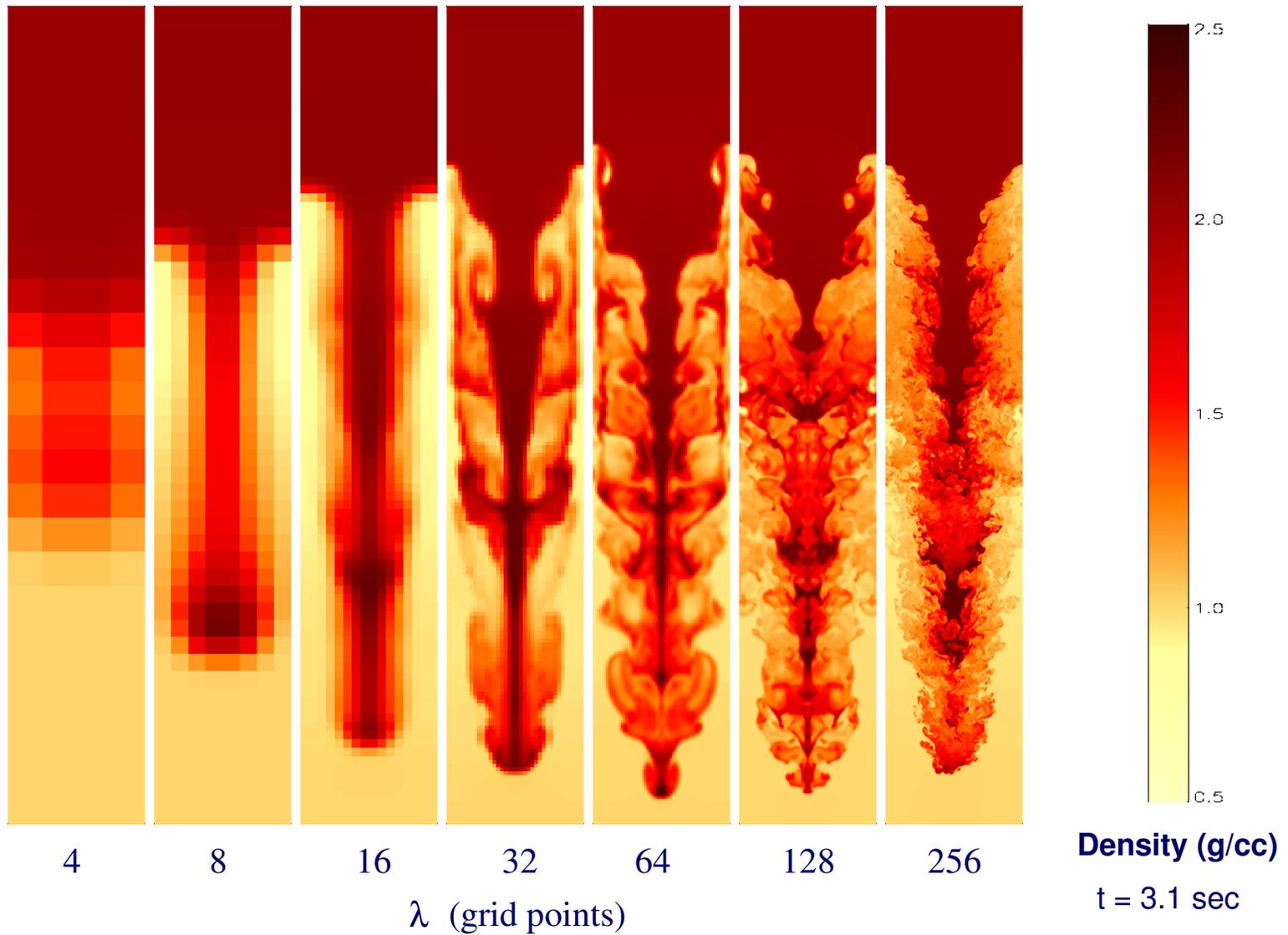


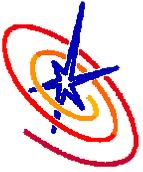
$$\alpha_{\text{spike}} = 0.058$$

$$\alpha_{\text{bubble}} = 0.052$$



# Single-mode 3-D Rayleigh-Taylor

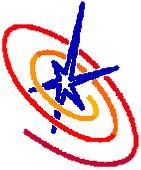




# Flash Exercises

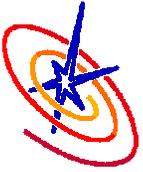
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- Set up and run the cellular detonation problem. Visualize the results with VisIt.
- Investigate differences between hydrodynamics solvers for the case of the Kelvin-Helmholtz instability.
- Two SN Ia related problems- thermonuclear flame and a detonation in a white dwarf.



# Thermonuclear Flame Setup

- Homework assignment: Starting with the Cellular detonation problem setup, modify it to simulate a deflagration.
  
- Hints:
  - What resolution?
  - How is a deflagration different from a detonation? More on this in the next lecture.
  - Only two files to modify:
    - `Simulation_initBlock.F90`
    - `flash.par`
  - Will need to use the (explicit) diffusion module. Do so with an option to the setup command.
  - `-with-unit=physics/Diffuse/DiffuseFluxBased`

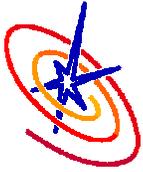


# White Dwarf Detonation Setup

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- Example of setting up a white dwarf model with a detonation.
- Hydro + burning + self-gravity.
- Test: Turn off burning. How long will the code hold the model steady?
- Note that there may be issues!
- Name of setup is SnDet.  

```
./setup SnDet -2d -auto -nxb=16 -nyb=16 +cylindrical  
-objdir=obj_SnDet
```
- Problem directories are in `source/Simulation/SimulationMain`



...and that leads us to

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## QUESTIONS AND DISCUSSION